

Strangeness:
a diagnostic tool of QGP

CIPPQG, September 5, 2001

WHY is strangeness a popular QGP diagnostic tool

EXPERIMENTAL REASONS

- Strange hadrons are subject to a self analyzing decay within a few cm from the point of production;
- Production rates hence statistical significance is high;
- There are many strange particles allowing to study different physics questions.

THEORETICAL CONSIDERATIONS

- ‘Accidental’ coincidence of scales: $m_s \simeq T_c \rightarrow \tau_s \simeq \tau_{\text{QGP}} \rightarrow$ strangeness a clock for reaction
- production of strangeness in gluon fusion $GG \rightarrow s\bar{s}$ strangeness linked to gluons from QGP;
- At SPS energy in baryon rich environment $\bar{s} > \bar{q} \rightarrow$ strange antibaryon enhancement and at RHIC (anti)hyperon dominance of (anti)baryons.

FORMATION OF STRANGENESS DENSE PHASE

NEAR Chemical strangeness equilibrium **REQUIRES QGP**: \Rightarrow

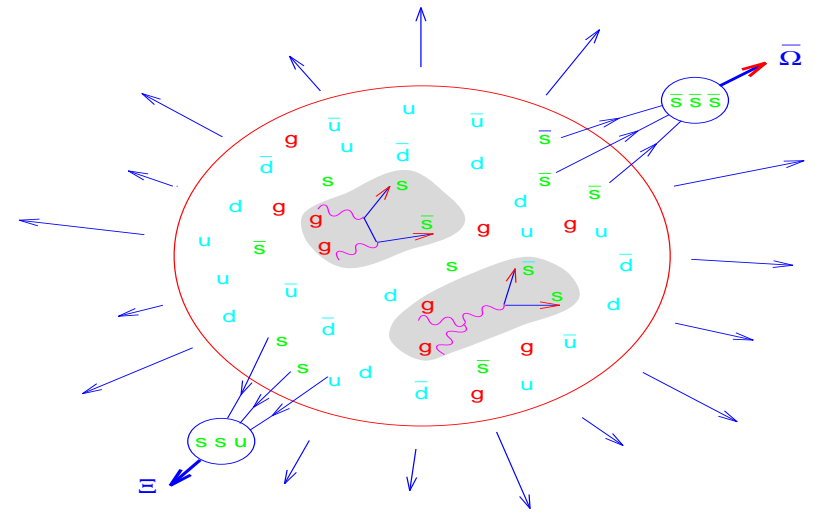
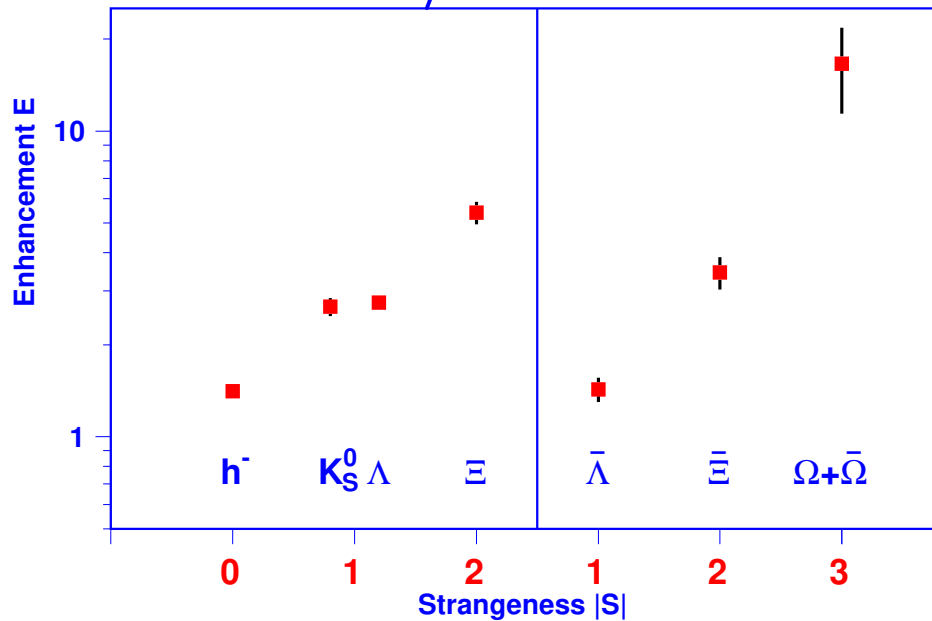
And produces observable excess of strangeness, and STRANGE ANTIBARYONS

(Rafelski 1980–82: summary in **Phys. Rep. 88 (1982) 331**)

How produced: In thermal QGP strangeness is dominantly produced by gluon fusion reactions $GG \rightarrow s\bar{s}$ (Rafelski/Müller, **PRL48 (1982) 1066**)

Kinetic processes in Hadron Gas too slow (Koch/Rafelski, **NP A444(1985) 678**)

WA97-SPS/CERN Results



Kinetic description of strangeness production

Kinetic equilibration is faster than chemical, use thermal particle distributions. Strange quark pair production dominated by **gluon fusion**: $G + G \rightarrow s\bar{s}$, add also some $q\bar{q} \rightarrow s\bar{s}$. Solve momentum-integrated Boltzmann equation:

$$\partial_\mu j_s^\mu \equiv \frac{\partial \rho_s}{\partial t} + \frac{\partial \vec{v} \rho_s}{\partial \vec{x}} = A^{gg \rightarrow s\bar{s}} + A^{q\bar{q} \rightarrow s\bar{s}} - A^{s\bar{s} \rightarrow gg, q\bar{q}}$$

$$A^{gg \rightarrow s\bar{s}} = \frac{1}{2} \rho_g^2(t) \langle \sigma v \rangle_T^{gg \rightarrow s\bar{s}}, \quad A^{q\bar{q} \rightarrow s\bar{s}} = \rho_q(t) \rho_{\bar{q}}(t) \langle \sigma v \rangle_T^{q\bar{q} \rightarrow s\bar{s}}, \quad A^{s\bar{s} \rightarrow gg, q\bar{q}} = \rho_s(t) \rho_{\bar{s}}(t) \langle \sigma v \rangle_T^{s\bar{s} \rightarrow gg, q\bar{q}}.$$

$$\langle \sigma v_{\text{rel}} \rangle_T \equiv \frac{\int d^3 p_1 \int d^3 p_2 \sigma_{12} v_{12} f(\vec{p}_1, T) f(\vec{p}_2, T)}{\int d^3 p_1 \int d^3 p_2 f(\vec{p}_1, T) f(\vec{p}_2, T)}.$$

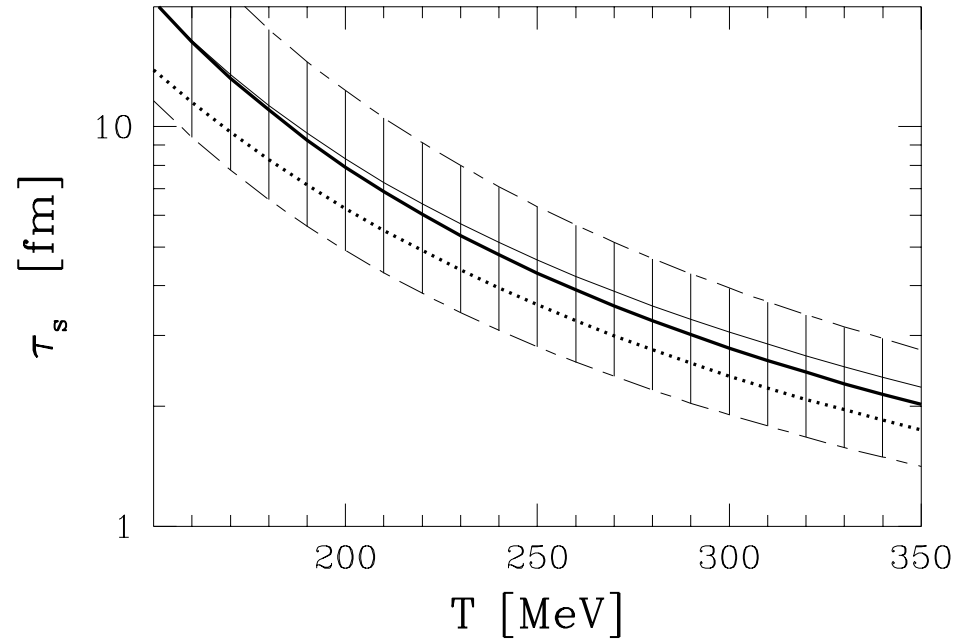
Exponential approach to chemical equilibrium $n_s(t)/n_s^\infty \rightarrow 1 - e^{-t/\tau_s}$ defines the characteristic time constant τ_s :

$$\tau_s \equiv \frac{1}{2(A^{gg \rightarrow s\bar{s}} + A^{q\bar{q} \rightarrow s\bar{s}} + \dots)} \frac{\rho_s^\infty}{\rho_s^\infty} \quad A^{12 \rightarrow 34} \equiv \frac{1}{1 + \delta_{1,2}} \rho_1^\infty \rho_2^\infty \langle \sigma_s v_{12} \rangle_T^{12 \rightarrow 34}.$$

$1/(1 + \delta_{1,2})$ introduced to compensate double-counting for identical particle pairs. **ENTROPY CONSERVING** expansion i.e. $T^3 V = \text{Const.}$ (not yet long. scaling):

$$2\tau_s \frac{dT}{dt} \left(\frac{d\gamma_s}{dT} + \frac{\gamma_s}{T} z \frac{K_1(z)}{K_2(z)} \right) = 1 - \gamma_s^2, \quad \gamma_s(t) \equiv n_s(t)/n_s^\infty, \quad z = \frac{m_s}{T}, \quad K_i : \text{Besself.}$$

Once γ_s known, $\langle s(t) \rangle = \langle \bar{s}(t) \rangle = \int dx^3 n_s^\infty(T(t, x)) \gamma_s(T(t, x), \vec{T}(t, x))$;
evolution till $t \rightarrow t_f$, but effectively production stops for $T < 180 \text{ MeV}$.



$\sigma_{\text{QCD}}^{\rightarrow s\bar{s}}$ gives τ_s similar to lifespan of the plasma phase! The generic angle averaged cross sections for (heavy) flavor s, \bar{s} production processes $g+g \rightarrow s+\bar{s}$ and $q+\bar{q} \rightarrow s+\bar{s}$,

$$\bar{\sigma}_{gg \rightarrow s\bar{s}}(s) = \frac{2\pi\alpha_s^2}{3s} \left[\left(1 + \frac{4m_s^2}{s} + \frac{m_s^4}{s^2} \right) \tanh^{-1}W(s) - \left(\frac{7}{8} + \frac{31m_s^2}{8s} \right) W(s) \right],$$

$$\bar{\sigma}_{q\bar{q} \rightarrow s\bar{s}}(s) = \frac{8\pi\alpha_s^2}{27s} \left(1 + \frac{2m_s^2}{s} \right) W(s). \quad W(s) = \sqrt{1 - 4m_s^2/s}$$

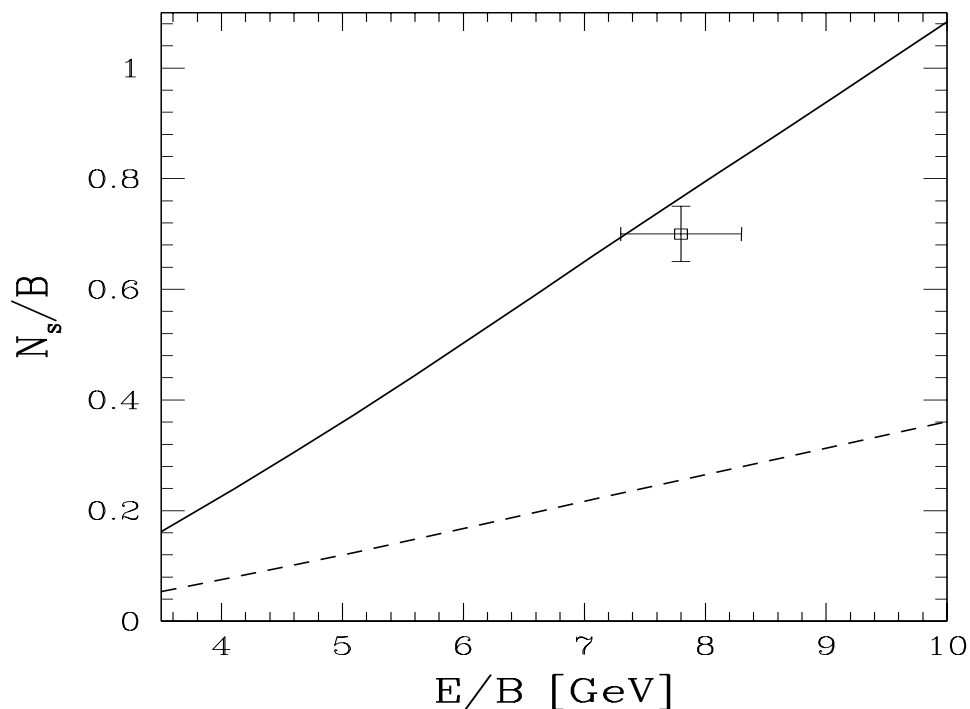
Infinite QCD resummation: running α_s and m_s taken at the energy scale $\mu \equiv \sqrt{s}$.

USED: $m_s(M_Z) = 90 \pm 20\%$ MeV

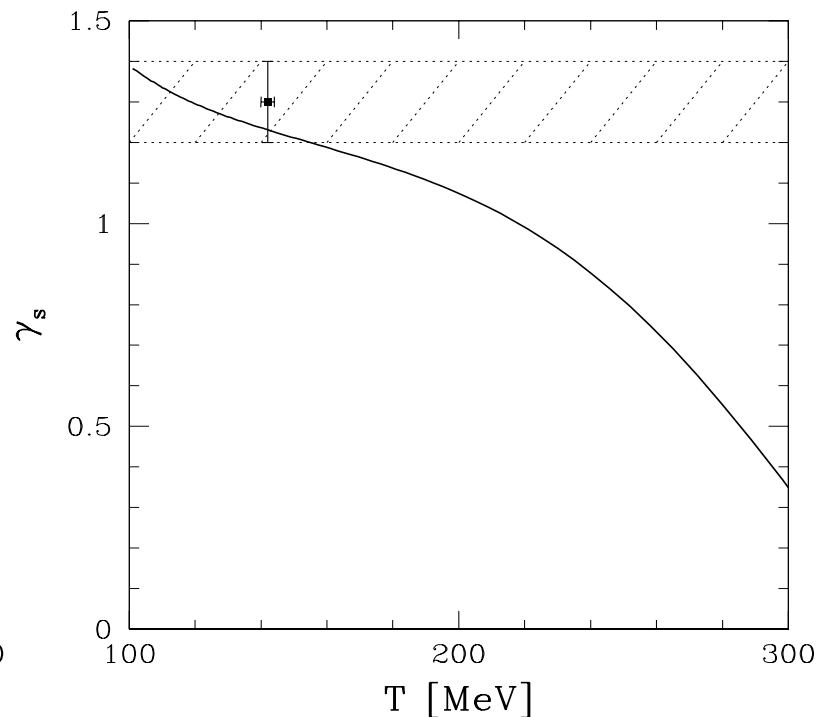
$m_s(1\text{GeV}) \simeq 2.1m_s(M_Z) \simeq 200\text{MeV}$.

Predictions of Kinetic Theory

SPECIFIC STRANGENESS YIELD



PHASE SPACE OCCUPANCY



s/B as function of energy per baryon E/B in the QGP fireball. The open square with error bars is result of our experimental data analysis compared to theory for γ_s , as function of temperature T , for $158A$ GeV Pb–Pb. Dashed curve: qualitative background illustration, given factor three central rapidity strangeness enhancement reported by WA97.

Key exp.result: High m_{\perp} slope universality

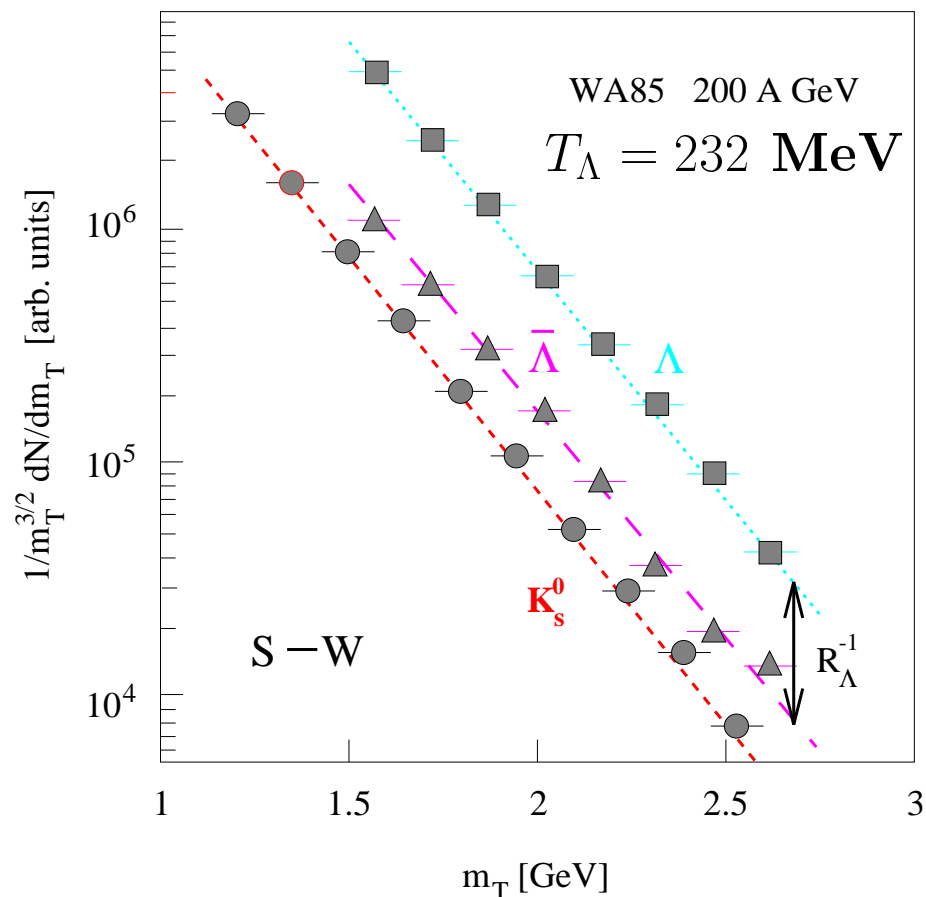
Discovered in S-induced collisions, very pronounced in Pb-Pb Interactions.

Why is the slope of baryons and antibaryons precisely the same?

Why is the slope of different particles in same m_t range the same?

Analysis+Hypothesis 1991:
QGP quarks coalescing in SUDDEN hadronization
(JR, PLB 262 (1991) 333.)

This allows to study ratios of particles measured only in a fraction of phase space



WA97	T_{\perp}^{Pb} [MeV]
T^{K^0}	230 ± 2
T^{Λ}	289 ± 3
$T^{\bar{\Lambda}}$	287 ± 4
T^{Ξ}	286 ± 9
$T^{\bar{\Xi}}$	284 ± 17
$T^{\Omega+\bar{\Omega}}$	251 ± 19

Λ within 1% of $\bar{\Lambda}$

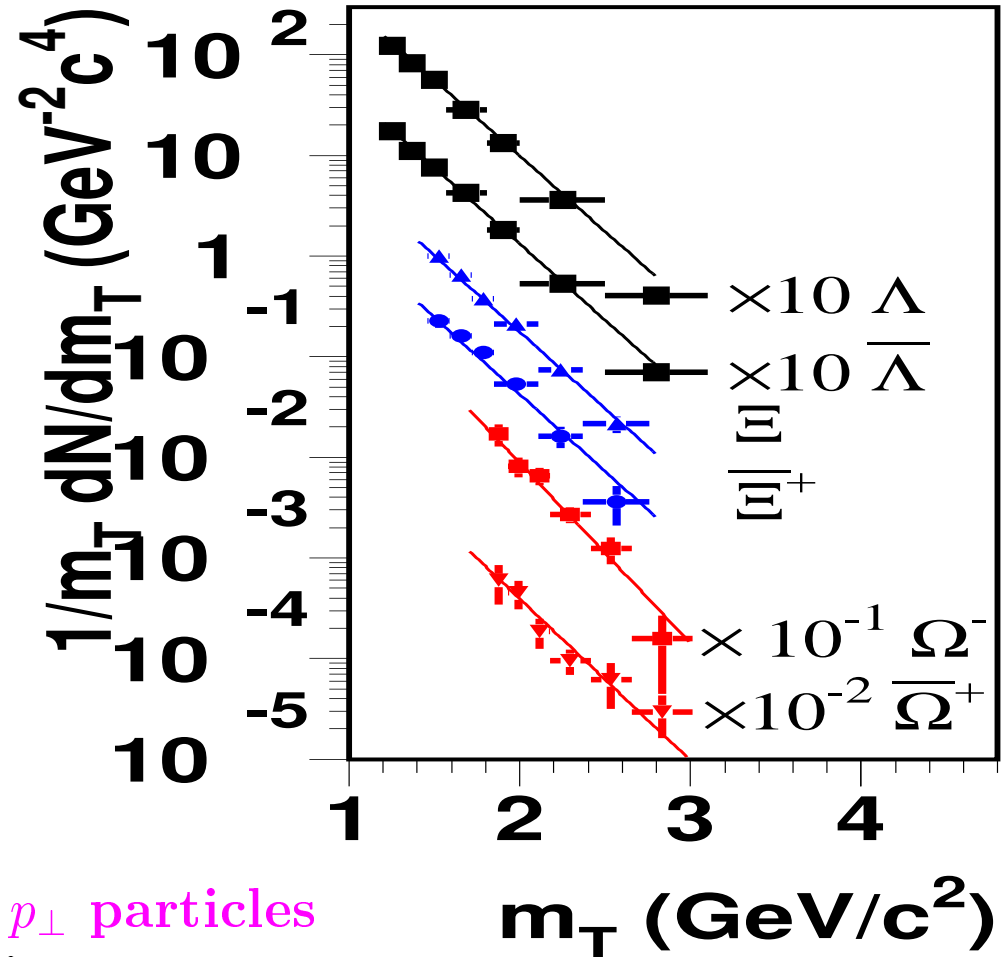
Kaon – hyperon difference:

EXPLOSIVE FLOW effect

Difference between $\Omega + \bar{\Omega}$:

presence of an excess of low p_{\perp} particles

we will return to study this in spectral analysis



1. Chemical freeze-out (T_f):

condition at which particle number stops changing

similar to early universe nucleosynthesis abundance freeze-out

2. **Later:** Thermal (kinetic) freeze-out (T_k):

condition at which particle momentum distribution stops evolving

similar to decoupling of cosmic background photons at $T = 3000K$

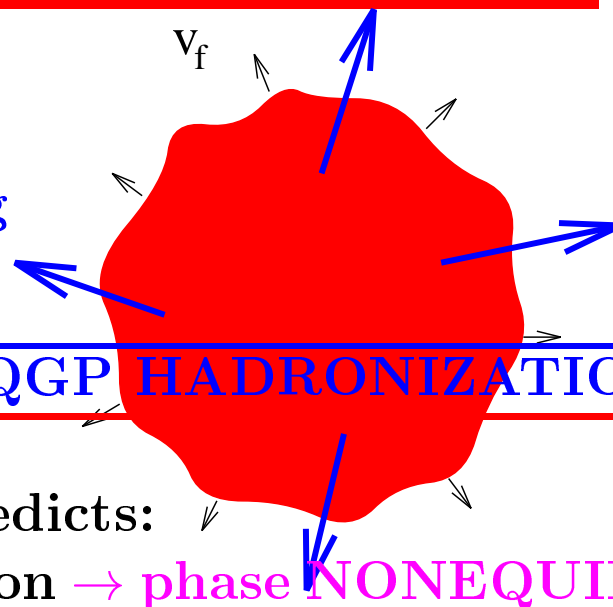
Since 1991: strange (anti)baryon production does not in detail follow hadron gas pattern: \rightarrow appear to be emitted directly by QGP

Potential to observe chemical properties of QGP

No hadronic 'phase'!

No 'mixed phase' either!

Direct emission of free-streaming hadrons from exploding QGP



Orient analysis towards SUDDEN QGP HADRONIZATION reaction

BUT: Phase equilibrium hydro predicts:

a slow transformation = contradiction \rightarrow phase NONEQUILIBRIUM

Super-cooling of a fast expanding fireball requires 1st order phase transition

P and ε : local in QGP particle pressure, energy density, \vec{v} local flow velocity. The pressure component in the energy-momentum tensor:

$$T^{ij} = P\delta_{ij} + (P + \varepsilon)\frac{v_i v_j}{1 - \vec{v}^2}.$$

The rate of momentum flow vector $\vec{\mathcal{P}}$ at the surface of the fireball is obtained from the energy-stress tensor T_{kl} :

$$\vec{\mathcal{P}} \equiv \hat{\mathcal{T}} \cdot \vec{n} = P\vec{n} + (P + \varepsilon)\frac{\vec{v}_c \vec{v}_c \cdot \vec{n}}{1 - \vec{v}_c^2}.$$

The pressure and energy comprise particle and the vacuum properties: $P = P_p - \mathcal{B}$, $\varepsilon = \varepsilon_p + \mathcal{B}$. Condition $\vec{\mathcal{P}} = 0$ reads:

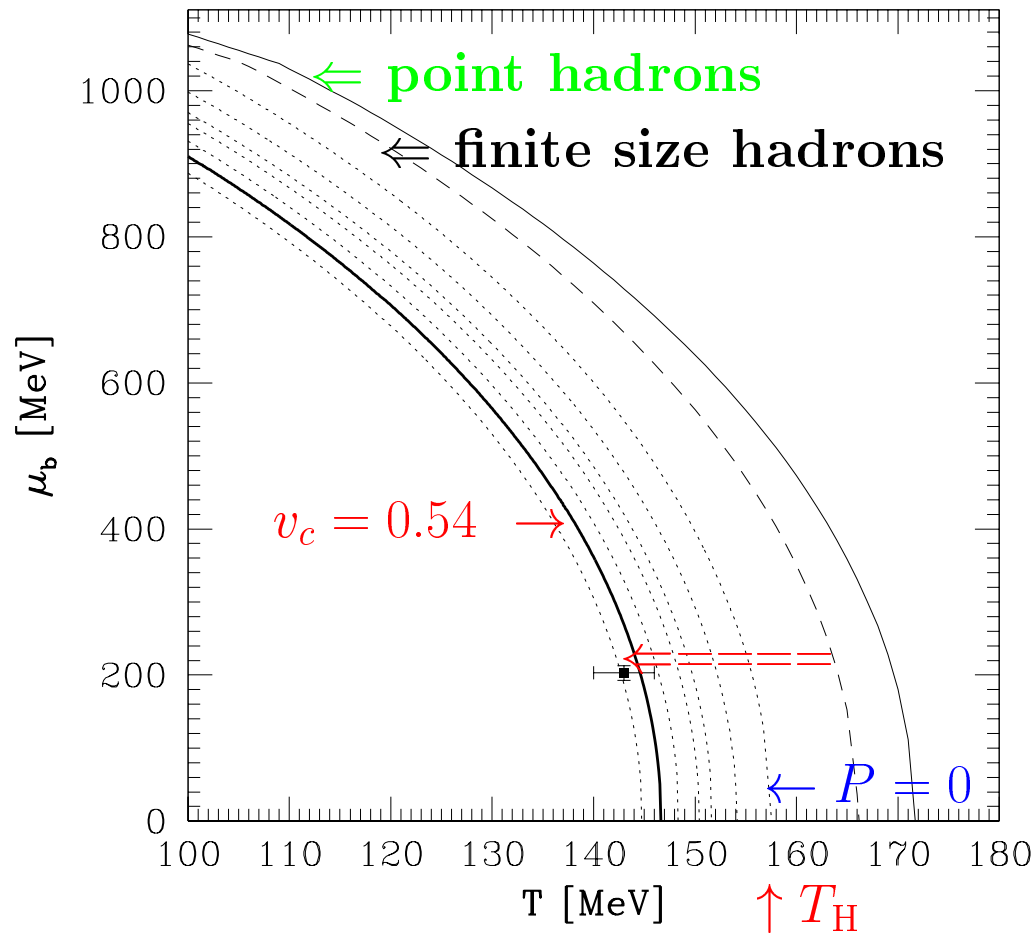
$$\mathcal{B}\vec{n} = P_p\vec{n} + (P_p + \varepsilon_p)\frac{\vec{v}_c \vec{v}_c \cdot \vec{n}}{1 - v_c^2},$$

Multiplying with \vec{n} , we find,

$$\mathcal{B} = P_p + (P_p + \varepsilon_p)\frac{\kappa v_c^2}{1 - v_c^2}, \quad \kappa = \frac{(\vec{v}_c \cdot \vec{n})^2}{v_c^2}.$$

This requires $P_p < \mathcal{B}$: QGP phase pressure P must be NEGATIVE. A fireball surface region which reaches $\mathcal{P} \rightarrow 0$ and continues to flow outwards is torn apart in a rapid instability. **This can arise since matter presses again the vacuum which is not subject to collective dynamics.**

Phase transition and SUDDEN breakup temperatures



Solid: point hadrons T_p

Dashed: finite size

Dotted: $T_c(\mu_b)|_{P_{eff}-B=0}$ for $v^2 = 0, 1/10, 1/6, 1/5, 1/4, 1/3$.

Thick solid: breakup with $v = 0.54$ ($\kappa = 0.6$)

PRL 85 (2000) 4695

DEEP SUPERCOOLING by 20 MeV

$T_H = 158$ MeV Hagedorn temperature where $P = 0$, no hadron P
 $T_f \simeq 0.9T_H \simeq 143$ MeV is where supercooled QGP fireball breaks up
 equilibrium phase transformation is at $\simeq 166$

Perturbative QCD EoS improved to agree with Lattice-QCD

$$\frac{T}{V} \ln \mathcal{Z}_{QGP} \equiv P = -\mathcal{B} + \frac{8}{45\pi^2} c_1 (\pi T)^4 + \frac{n_q}{15\pi^2} \left[\frac{7}{4} c_2 (\pi T)^4 + \frac{15}{2} c_3 \left(\mu_q^2 (\pi T)^2 + \frac{1}{2} \mu_q^4 \right) \right],$$

$$c_1 = 1 - \frac{15\alpha_s}{4\pi}, \quad c_2 = 1 - \frac{50\alpha_s}{21\pi}, \quad c_3 = 1 - \frac{2\alpha_s}{\pi}.$$

$$\mu \frac{\partial \alpha_s}{\partial \mu} = -b_0 \alpha_s^2 - b_1 \alpha_s^3 + \dots \equiv \beta_2^{\text{pert}}, \quad b_0 = \frac{11 - 2n_f/3}{2\pi}, \quad b_1 = \frac{51 - 19n_f/3}{4\pi^2}.$$

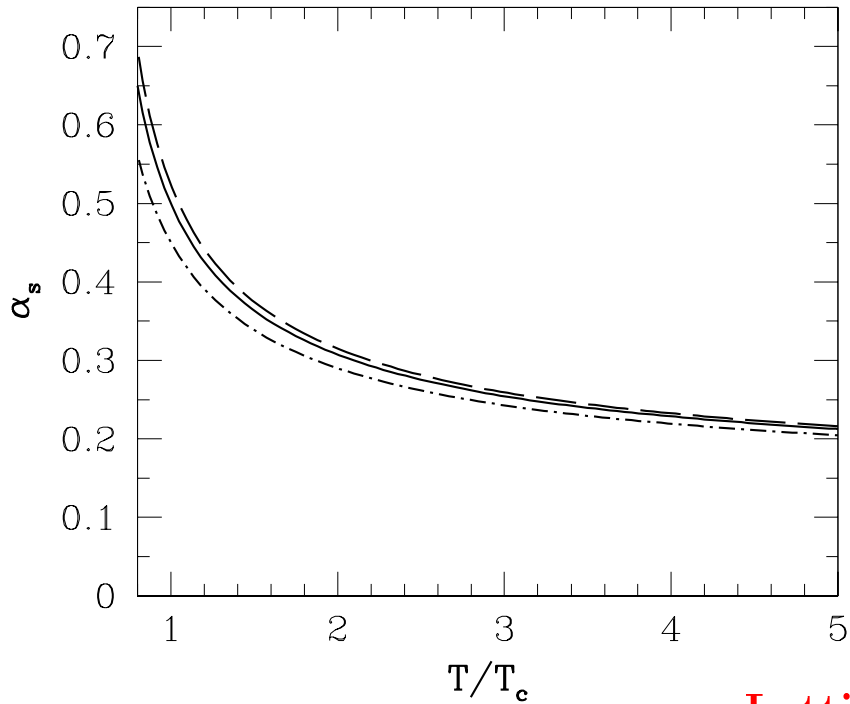
where $\alpha_s(\mu = M_Z) = 0.118 + 0.001 - 0.0016$.

$$\alpha_s/\pi < 0.22$$

$$\mu = 2\pi\beta^{-1} \sqrt{1 + \frac{1}{\pi^2} \ln^2 \lambda_q} = 2\sqrt{(\pi T)^2 + \mu_q^2}.$$

just a little **WORK** to test how this compares to lattice ($\mu_b = 0$)

Pressure of QGP-Liquid

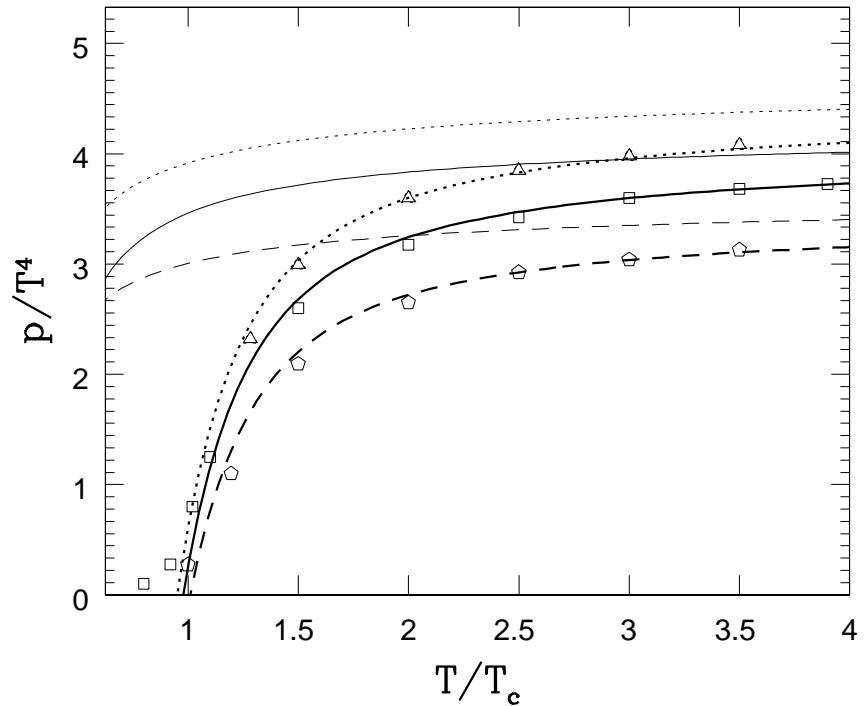


$\alpha_s(2\pi T)$ for $T_c = 0.16$ GeV.

Dashed line: $\alpha_s(M_Z) = 0.119$;

solid line = 0.118;

dot-dashed = 0.1156.



Lattice-QCD results F. Karsch, E. Laermann and A. Peikert *Phys. Lett. B* 478, 447-455, (2000);

Quark-gluon liquid model at $\lambda_q = 1$ (thick lines) and with $\mu = 2\pi T = \kappa T/T_c$, $\kappa = 1$ GeV. $\mathcal{B} = 0.19$ GeV/fm³.

Solid line 2+1 flavors ($m_s/T = 1.7$), dotted 3 flavors, dashed 2 flavors.

Thin lines: with approximate 2nd order α_s (often used comparison):

Extension to finite baryon density

To relate the QCD scale to the temperature $T = 1/\beta$ we use

$$\mu = 2\sqrt{(\pi T)^2 + \mu_q^2} = 2\pi\beta^{-1}\sqrt{1 + \frac{1}{\pi^2}\ln^2\lambda_q}.$$

A convenient way to obtain entropy and baryon density uses the thermodynamic potential \mathcal{F} :

$$\frac{\mathcal{F}(T, \mu_q, V)}{V} = -\frac{T}{V} \ln \mathcal{Z}(\beta, \lambda_q, V)_{\text{QGP}} = -P_{\text{QGP}}.$$

The entropy density is:

$$s_{\text{QGP}} = -\frac{d\mathcal{F}}{VdT} = \frac{32\pi^2}{45}c_1T^3 + \frac{n_f7\pi^2}{15}c_2T^3 + n_fc_3\mu_q^2T + A\frac{\pi^2T}{\pi^2T^2 + \mu_q^2}.$$

Noting that baryon density is 1/3 of quark density, we have:

$$\rho_B = -\frac{1}{3}\frac{d\mathcal{F}}{Vd\mu_q} = \frac{n_f}{3}c_3\left\{\mu_qT^2 + \frac{1}{\pi^2}\mu_q^3\right\} + \frac{1}{3}A\frac{\mu_q}{\pi^2T^2 + \mu_q^2}.$$

$$A = A_g + A_q + A_s; \quad A_g = (b_0\alpha_s^2 + b_1\alpha_s^3)\frac{2\pi}{3}T^4$$

$$A_{i=q,s} = (b_0\alpha_s^2 + b_1\alpha_s^3)\left[\frac{n_i5\pi}{18}T^4 + \frac{n_i}{\pi}\left\{\mu_i^2T^2 + \frac{1}{2\pi^2}\mu_i^4\right\}\right].$$

OBJECTIVE: is to describe the phase space of hadronic particles in great precision, not to fit the data. Physics in parameters of the phase space, thus χ^2/dof must promise physical relevance.

Chemical Freeze-Out: FERMI 2001 MODEL

The thermal emitted particles production yield dN_i within the time

T_f	Local rest frame chemical freeze-out temperature
v_h, v_f	Hadronization, Local flow speed of emitting source
λ_s, λ_q	Chemical fugacities describe conserved quantum number
γ_s, γ_q	Phase space occupancies describe quark pair yield

dt from a locally at rest surface element dS :

$$dN_i = \frac{dS d^3p}{(2\pi)^3} A_i v_i dt .$$

$v_i = dz/dt$ is the particle velocity normal to the surface element dS .

In a thermal quark-gluon source, phase space factor A_i is:

$$A_i = g_i \lambda_i \gamma_i e^{-E_i/T} , \quad \lambda_i = \prod_{j \in i} \lambda_j , \quad \gamma_i = \prod_{j \in i} \gamma_j , \quad E_i = \sum_{j \in i} E_j ,$$

g_i is the degeneracy of the produced particle, and E_i its energy:

$$E_j = \sqrt{m_j^2 + p^2} = \sqrt{m_j^2 + p_{\perp}^2} \cosh(y - y_{\text{CM}}) .$$

HOW DOES THE MODEL WORK?

$$R_\Lambda = \frac{\overline{\Lambda}}{\Lambda} \Big|_{m_\perp} = \frac{\overline{\Lambda} + \overline{\Sigma}^0 + \overline{\Lambda}^* + \dots}{\Lambda + \Sigma^0 + \Lambda^* + \dots} = \frac{\overline{s\bar{q}\bar{q}}}{sq\bar{q}} = \lambda_s^{-2} \lambda_q^{-4}.$$

$$R_\Xi = \frac{\overline{\Xi^-}}{\Xi^-} \Big|_{m_\perp} = \frac{\overline{\Xi^-} + \dots}{\Xi^- + \dots} = \frac{\overline{s\bar{s}\bar{q}}}{ssq} = \lambda_s^{-4} \lambda_q^{-2}.$$

$$\frac{\Xi^-(dss)}{\Lambda(dd\bar{s})} \Big|_{m_\perp} = \frac{g_\Xi \gamma_d \gamma_s^2 \lambda_d \lambda_s^2}{g_\Lambda \gamma_d^2 \gamma_s \lambda_d^2 \lambda_s}.$$

g_i are the spin statistical factors of the states considered.

$$\frac{\overline{\Xi^-(dss)}}{\overline{\Lambda(dd\bar{s})}} \Big|_{m_\perp} = \frac{g_\Xi \gamma_d \gamma_s^2 \lambda_d^{-1} \lambda_s^{-2}}{g_\Lambda \gamma_d^2 \gamma_s \lambda_d^{-2} \lambda_s^{-1}}.$$

EXAMPLE: Pb–Pb ANALYSIS Fermi-2000 Model

Pb–Pb 158A GeV WA97 (top) and NA49 (bottom) S'2000 revised data
particle ratios by:

References

- [1] I. Králik, WA97,
Nucl. Phys. A 638,115, (1998).
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Phys. Rev. Lett. 82, 2471 (1999).

Ratios	Ref.	Exp. Data	Pb _v ^{S,γq}	Pb _v ^{γq}
Ξ/Λ	[1]	0.099 ± 0.008	0.098	0.096
$\bar{\Xi}/\bar{\Lambda}$	[1]	0.203 ± 0.024	0.199	0.201
$\bar{\Lambda}/\Lambda$	[1]	0.124 ± 0.013	0.122	0.121
$\bar{\Xi}/\Xi$	[1]	0.255 ± 0.025	0.248	0.253
$\frac{(\Xi+\bar{\Xi})}{(\Lambda+\bar{\Lambda})}$	[2]	0.13 ± 0.03	0.111	0.110
K^0/ϕ	[3]	11.9 ± 1.5	13.0	13.4
ϕ/π^-	[5]	0.0125 ± 0.0018	0.0127	0.0124
K^+/K^-	[4]	1.80 ± 0.10	1.757	1.790
p/\bar{p}	[6]	$18.1 \pm 4.$	16.00	16.50
$\bar{\Lambda}/\bar{p}$	[7]	$3. \pm 1.$	0.53	0.54
K^{\pm}/π^-		0.082 ± 0.012	0.81	0.080
K_s^0/B	[8]	0.183 ± 0.027	0.188	0.192
h^-/B	[9]	1.97 ± 0.1	1.782	1.829
		χ^2_{T}	2.25	1.36
		$N; p; r$	10;3;2	10;4;2
$\chi^2_{\text{T}}/\text{dof}$		LESS than	0.25	0.15

Chemical and Physical Properties for Pb–Pb and for S–Au/W/Pb

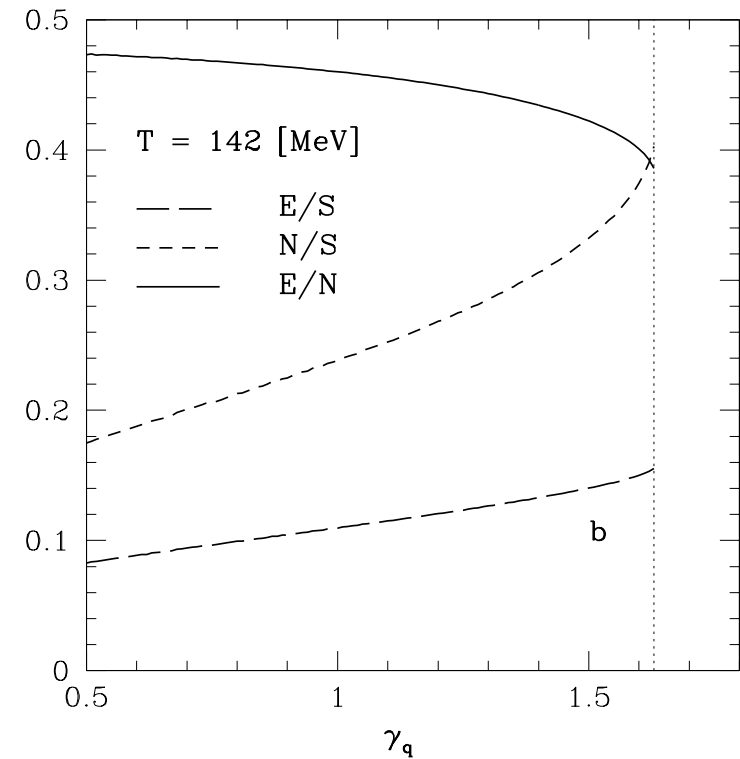
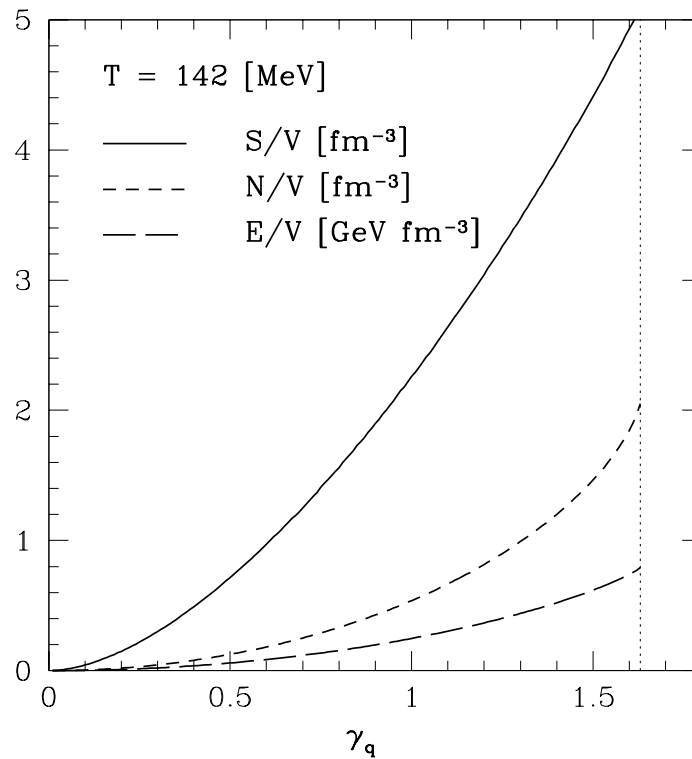
	Pb $^s_{ v} \gamma_q$	Pb $^{\gamma_q}_{ v}$	S $^s_{ v}$
$\chi^2_{\text{T}}; N; p; r$	1.48; 11; 3; 2	0.76; 11; 4; 2	6.2; 16; 6; 6
T_f [MeV]	151 ± 3	147 ± 5.5	144 ± 2
v_c	0.57 ± 0.05	0.52 ± 0.09	0.49 ± 0.02
λ_q	1.618 ± 0.026	1.625 ± 0.025	1.51 ± 0.02
λ_s	1.101^*	1.093 ± 0.02	1.00 ± 0.02
γ_q	$\gamma_q^{c*} = e^{m_\pi/2T_f} = 1.59$	$\gamma_q^{c*} = e^{m_\pi/2T_f} = 1.62$	1.41 ± 0.08
γ_s/γ_q	1.04 ± 0.05	1.05 ± 0.06	0.69 ± 0.03
E_f^{in}/S_f	0.163 ± 0.01	0.158 ± 0.01	0.186 ± 0.01
s_f/b	0.68 ± 0.05	0.69 ± 0.05	0.73 ± 0.05
$(\bar{s}_f - s_f)/b$	0^*	0.05 ± 0.05	0.17 ± 0.05

WHY $\gamma_q \simeq 1.6$? A striking feature of the data analysis is the maximization of entropy density in pion gas.

$$E_\pi = \sqrt{m_\pi^2 + p^2}$$

$$S_{B,F} = \int \frac{d^3p d^3x}{(2\pi\hbar)^3} [\pm(1 \pm f) \ln(1 \pm f) - f \ln f], \quad f_\pi(E) = \frac{1}{\gamma_q^{-2} e^{E_\pi/T} - 1}.$$

Pion gas properties: N -particle, E -energy, S -entropy, V -volume as function of γ_q .



CONCLUSION: excess of QGP entropy pumped into pions

The Omega Question Chemical analysis DOES NOT INCLUDE Ω -yield. Thermal analysis shows excess of Ω and $\bar{\Omega}$ at soft momentum, This means that these MOST RARELY produced strange hadrons are sensitive to NEW formation channels beyond the statistical Fermi model hadron phase space.

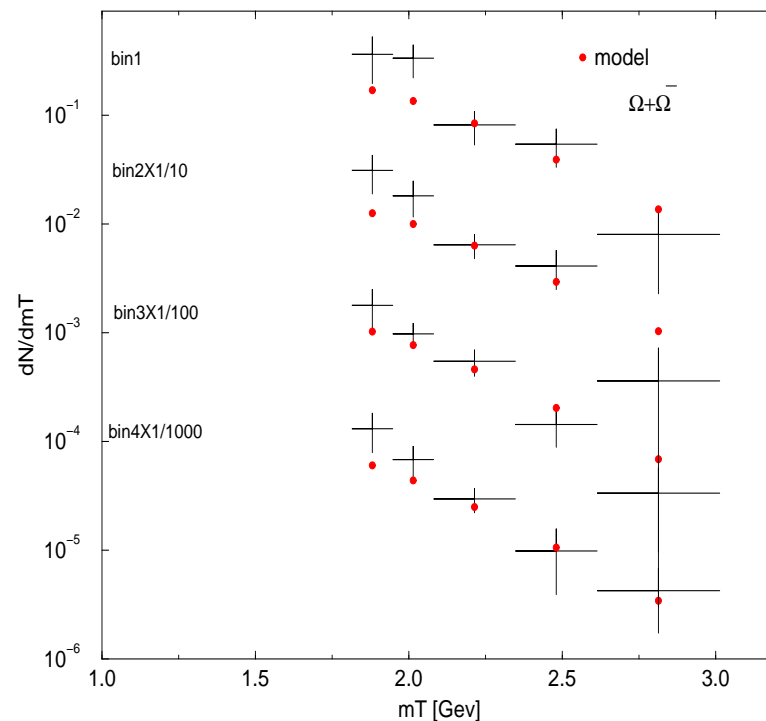
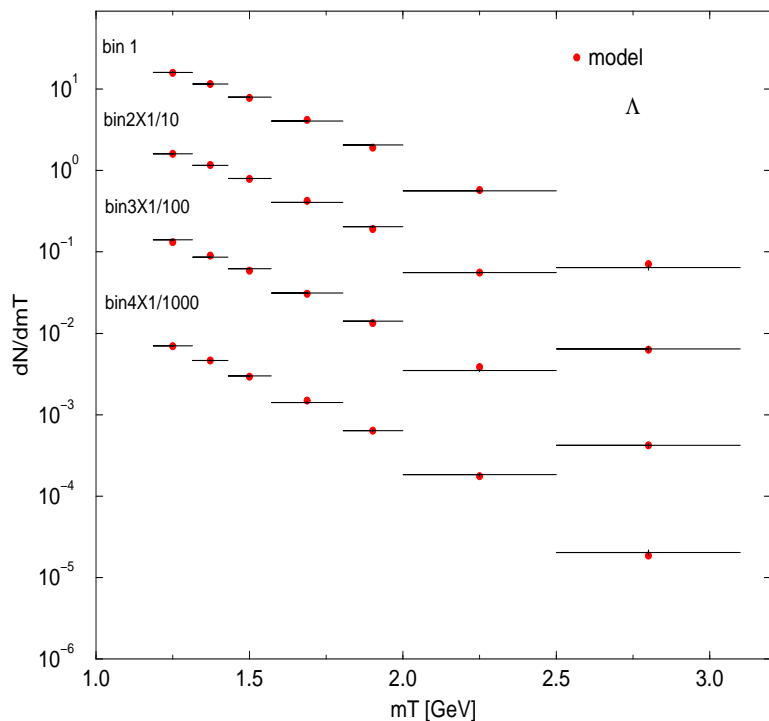
Significant contributions can arise from:

1. in source $(ss)_{\bar{3}}$ and $(\bar{s}\bar{s})_3$ clusters (predicted);
2. formation in final state fragmentation $(\bar{s}\bar{s})_3 + G \rightarrow (\bar{s}\bar{s}\bar{s}) + X$;
3. chiral disoriented strangeness vacuum (Kapusta/Wang PRL);

A way to see if two first hypothesis for extra Ω and $\bar{\Omega}$ can work is to see if one extra parameter explains 3 data points (ratios $\bar{\Omega}/\Omega$, Ω/Ξ , $\bar{\Omega}/\bar{\Xi}$). We find that $40 \pm 10\%$ of Ξ and $\bar{\Xi}$ clusters has to turn into Ω and $\bar{\Omega}$ to obtain the required additional yields ($\chi^2 \simeq 0.1!$)

None of the global properties (strangeness conservation etc) is affected by this ‘inperfection’ of the statistical phase space hadronization model.

COMPARE m_{\perp} SPECTRA



Thermal analysis of Λ (left) and $\Omega + \bar{\Omega}$ (right) m_T spectra. 'dots' theoretical values; Histogram lines: WA97 DATA obtained in different centrality bins. Note for $\Omega + \bar{\Omega}$ at low m_{\perp} the systematic difference between thermal de facto prediction and experiment.

TOPIS FOR DISCUSSION: HOW STRANGENESS DEFINES QGP

In past 20 years we reached understanding of strangeness kinetic evolution

Dynamics: SUPERCOOLED QGP FIREBALL BREAKS SUDDENLY

**Analysis of data: PRECISE DESCRIPTION OF FINAL STATE REQUIRED
YIELD NON-EQUILIBRIUM REQUIRES PARTICLE ABUNDANCES
PARAMETERS**

CHEMICAL PROPERTIES IN SUDDEN BREAKUP:

$$\tilde{\lambda}_s = 1, \quad \gamma_q \rightarrow e^{m_\pi/T}, \quad \gamma_s > 1$$

conservation of strangeness and maximum of entropy lead to these values

Evidence for non-statistical production of $\Omega(sss)$

CHEMICAL AND THERMAL FREEZE-OUT ANALYSIS COINCIDE

**STRANGE HADRON RESONANCE DIAGNOSIS OF SUDDEN
HADRONIZATION**

**RHIC HADRONS SIMILAR TO SPS BUT EXPECT BARYONS
DOMINATED BY HYPERONS**

Remember: universality of baryon/antibaryon slopes before asking a question

Thermal FREEZE-OUT Analysis

Hadron m_{\perp} -spectra are result of flow and thermal motion and are strongly influenced by resonance decays. The Flow-Boltzmann distribution we adapt with two velocities, one local temperature:

$$\frac{d^2 N}{dm_T dy} \propto \left(1 - \frac{\vec{v}_f^{-1} \cdot \vec{p}}{E} \right) \gamma m_T \cosh y e^{-\gamma \frac{E}{T} \left(1 - \frac{\vec{v} \cdot \vec{p}}{E} \right)}, \quad \gamma = 1/\sqrt{1-v^2}$$

Resonance 2-body decay contribution:

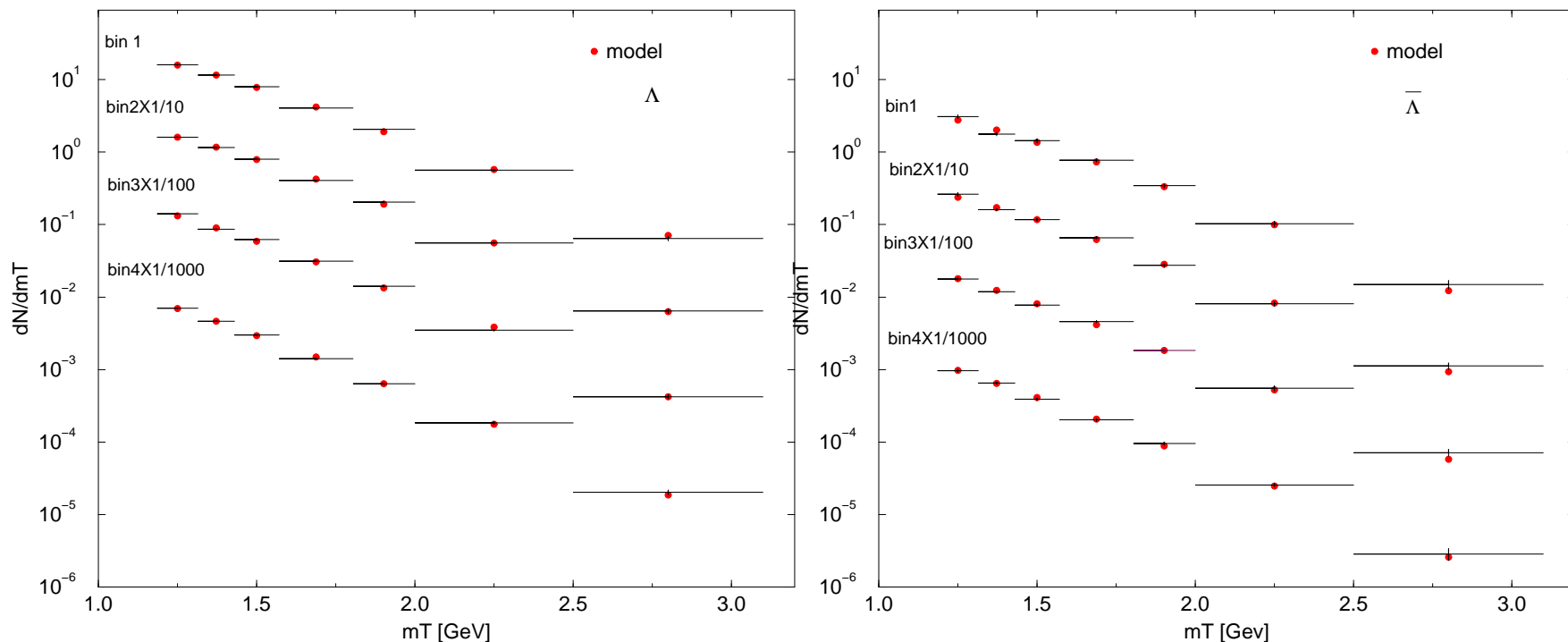
$$\frac{dN_X}{dm_{\perp}} = \frac{dN_X}{dm_{\perp}} \Big|_{\text{direct}} + \sum_{\forall R \rightarrow X+2+\dots} \frac{dN_X}{dm_{\perp}} \Big|_{R \rightarrow X+2+\dots}, \quad \frac{dN_X}{dm_{\perp}^2 dy} = \frac{g_r b}{4\pi p^*} \int_{Y_-}^{Y_+} dY \int_{M_{T-}}^{M_{T+}} dM_T^2 J \frac{d^2 N_R}{dM_T^2 dY}.$$

$$J = \frac{M}{\sqrt{P_T^2 p_T^2 - \{ME^* - M_T m_T \cosh \Delta Y\}^2}}, \quad \Delta Y = Y - y, \quad E^* = (M^2 - m^2 - m_2^2)/2M,$$

$$p^* = \sqrt{E^{*2} - m^2}$$

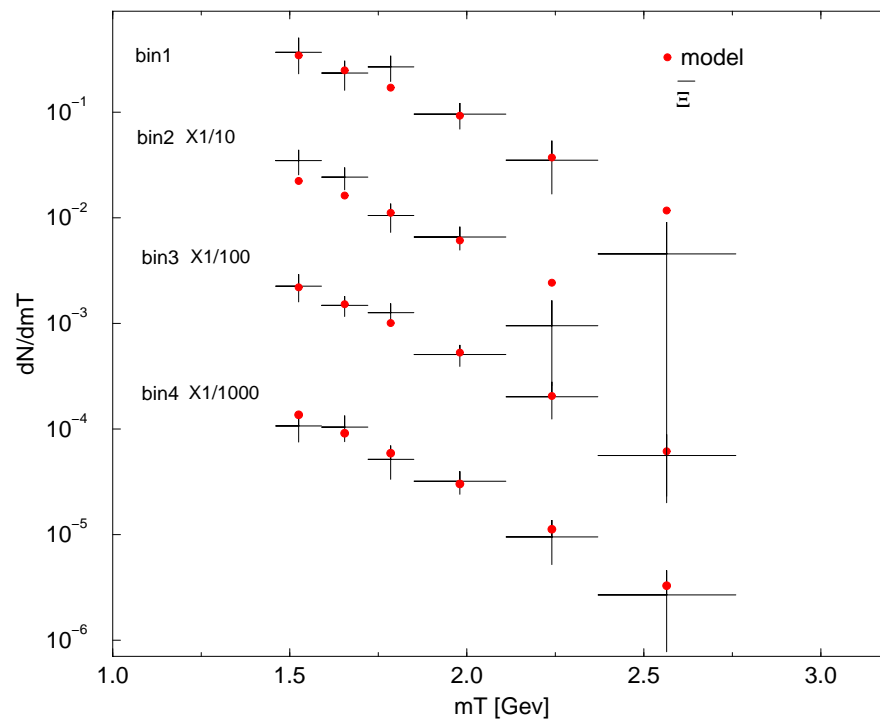
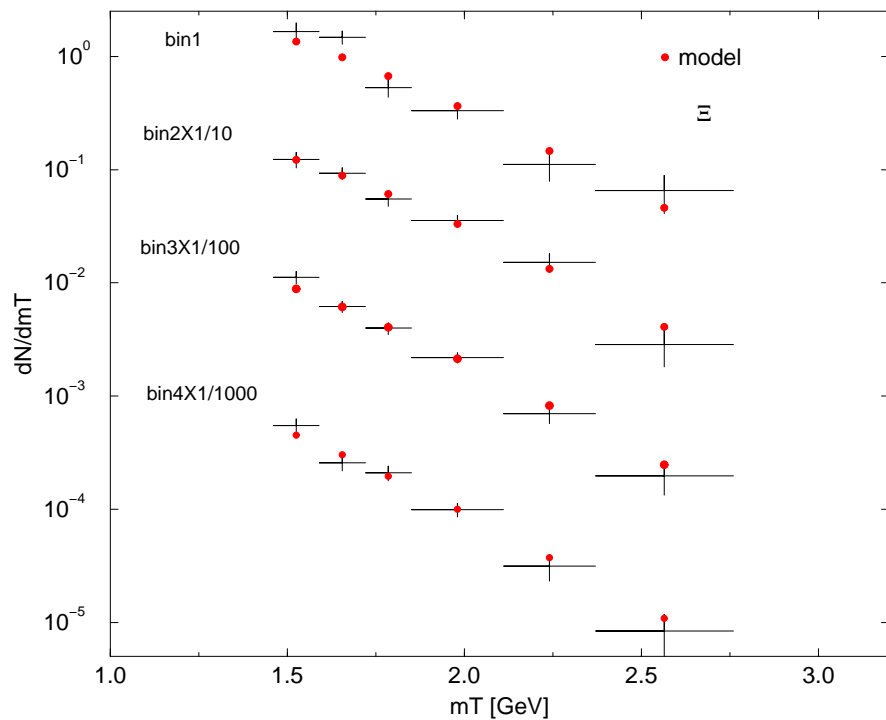
$$Y_{\pm} = y \pm \sinh^{-1} \left(\frac{p^*}{m_T} \right), \quad M_{T\pm} = M \frac{E^* m_T \cosh \Delta Y \pm p_T \sqrt{p^{*2} - m_T^2 \sinh^2 \Delta Y}}{m_T^2 \sinh^2 \Delta Y + m^2}$$

Λ and $\bar{\Lambda} - m_{\perp}$ SPECTRA



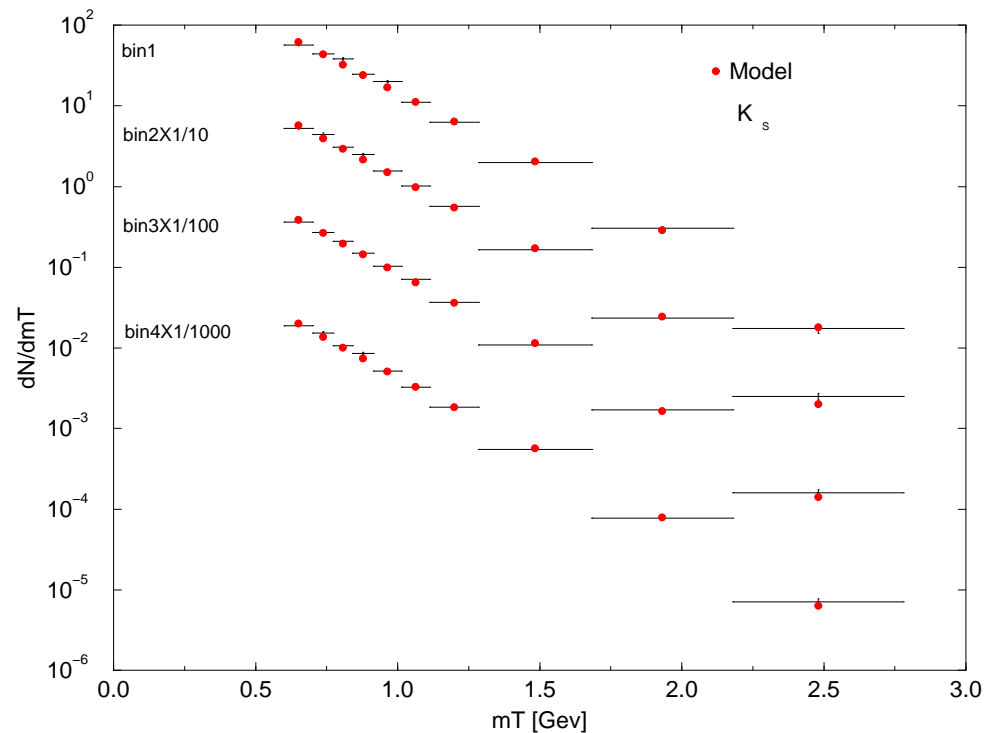
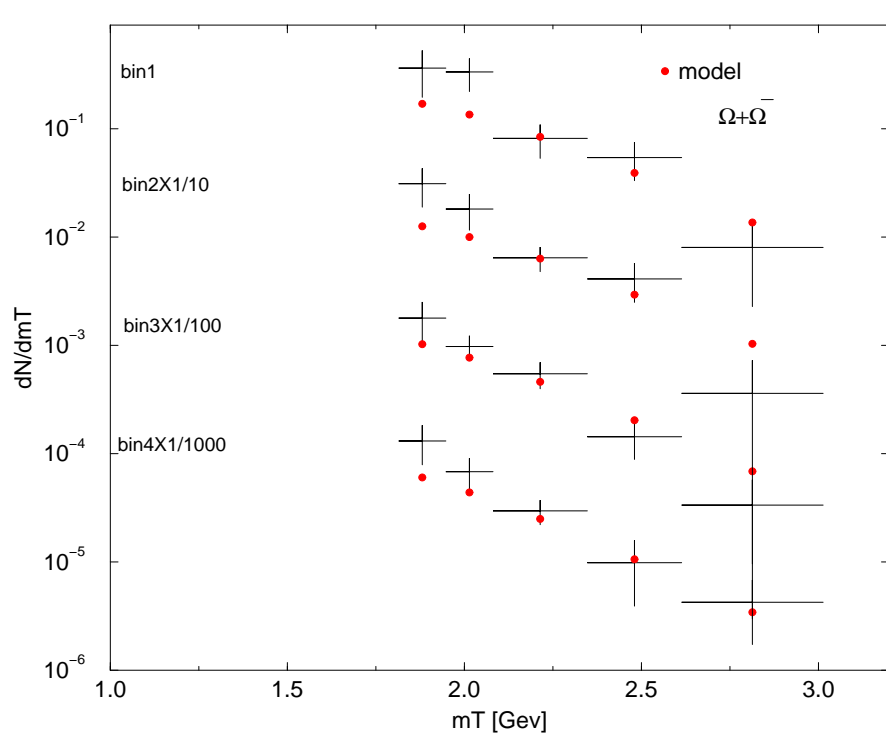
Thermal analysis m_T spectra: Λ (left) and $\bar{\Lambda}$ (right) for 4 different centralities.
 ‘dots’ theoretical values; HISTOGRAM: WA97 data in different centrality bins.

Ξ and $\Xi - m_{\perp}$ SPECTRA



Thermal analysis m_T spectra: Ξ (left) and $\Xi - m_{\perp}$ (right) for 4 different centralities. 'dots' theoretical values; Histogram lines: WA97 data in different centrality bins.

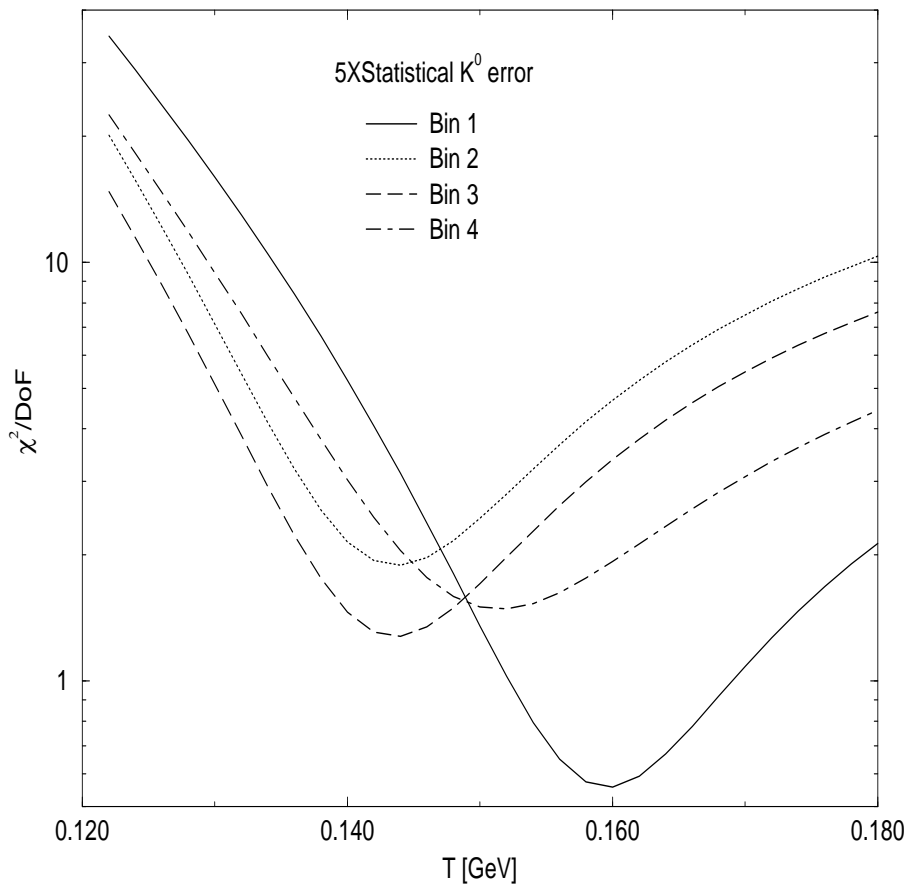
$\Omega + \bar{\Omega} - m_{\perp}$ and K_s -SPECTRA



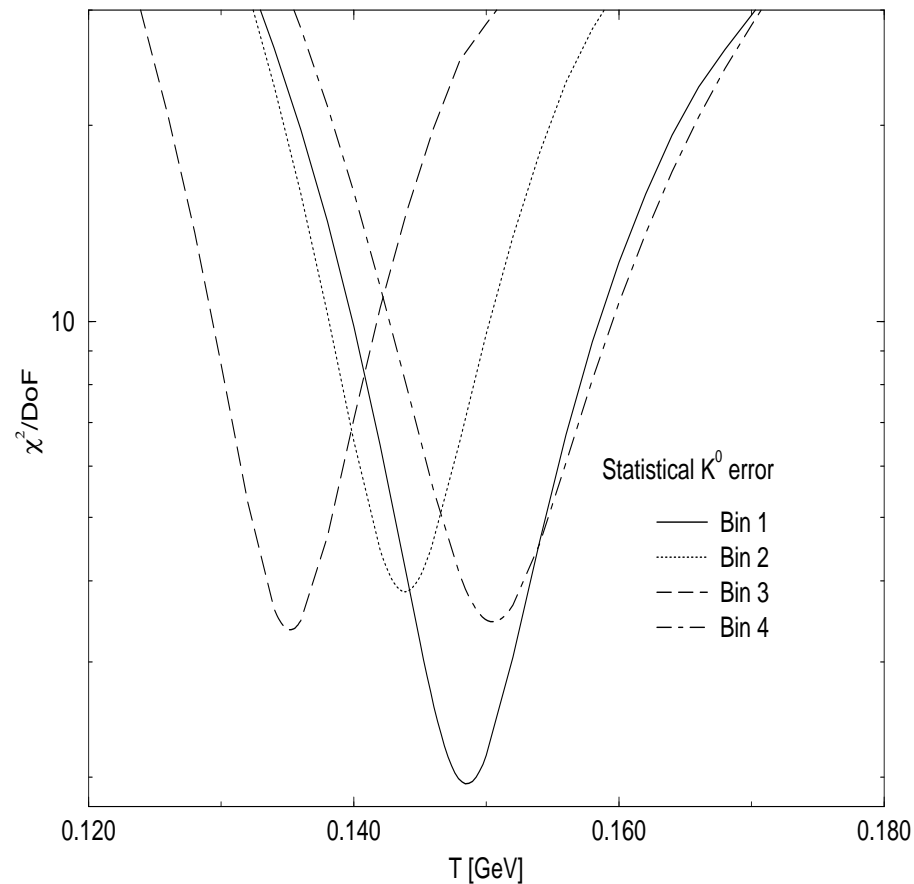
‘dots’ theoretical values; Histogram WA97 DATA

We systematically under predict $\Omega + \bar{\Omega}$ for the two lowest m_{\perp} data points. We recall that there is a disagreement with the Omega yields in the chemical analysis, here we see that this disagreement is arising at low momentum. **NEED:** a soft momentum secondary source.

The χ^2 profiles show good significance, here TEMPERATURE T :
 Total error divided by degrees of freedom for five centrality bins

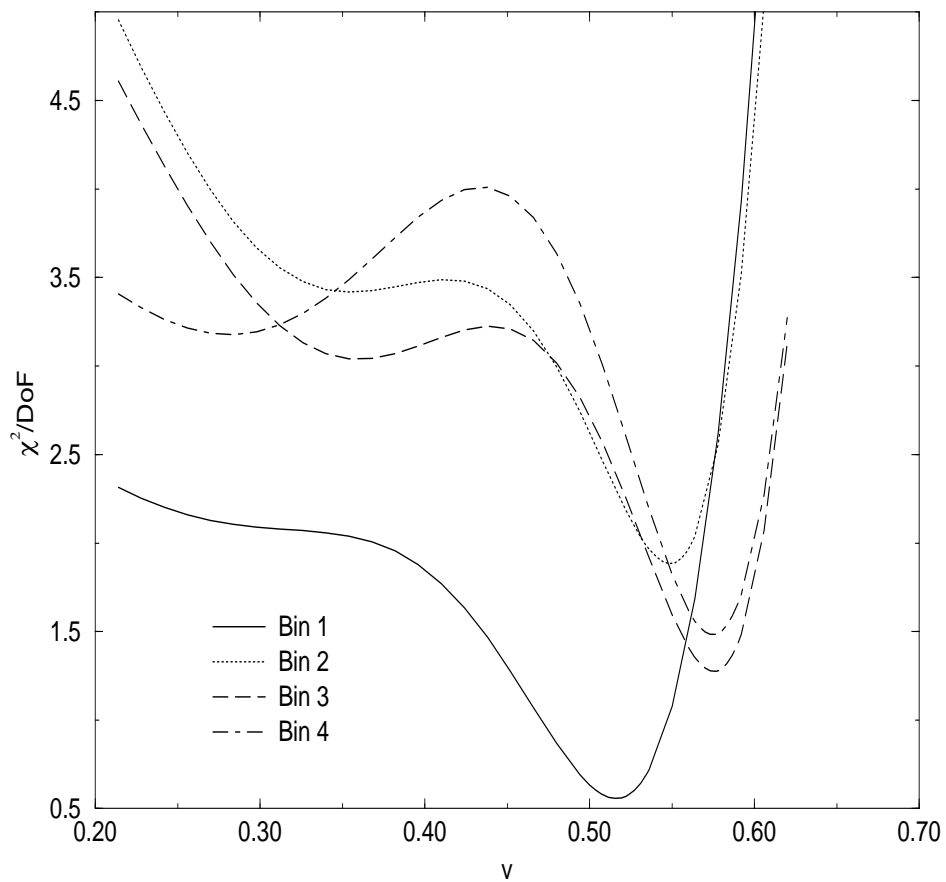


5 times enlarged K^0 stat. error

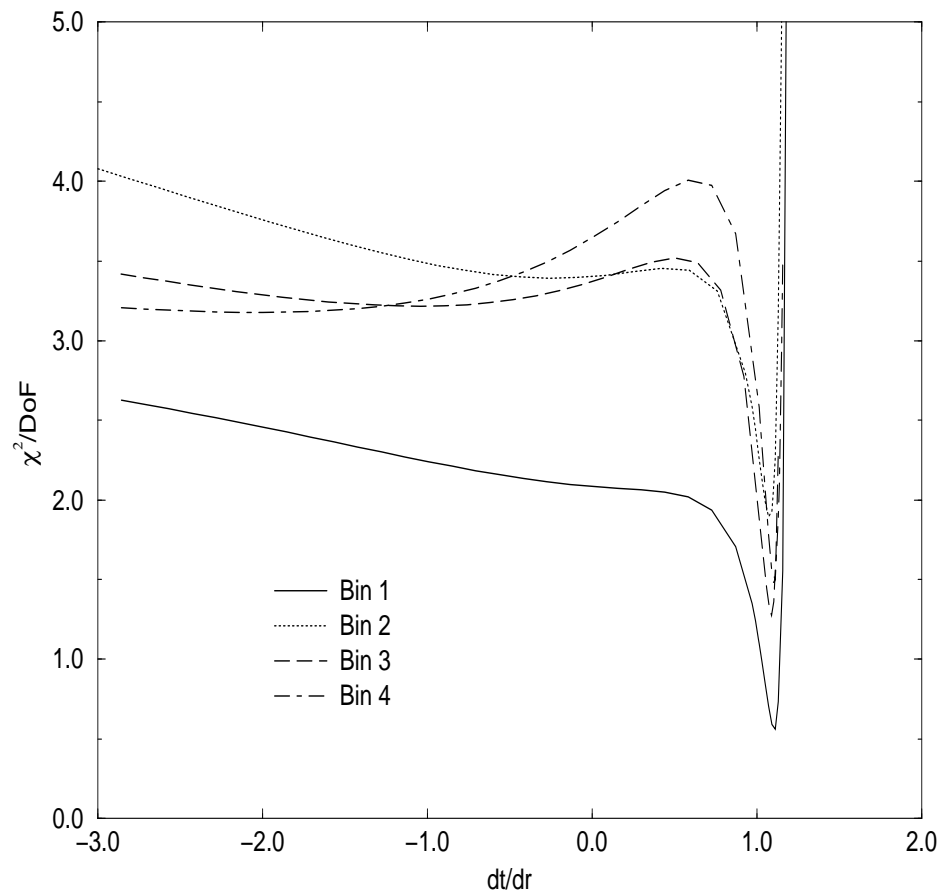


experimental stat. K^0 error.

here v on LEFT and

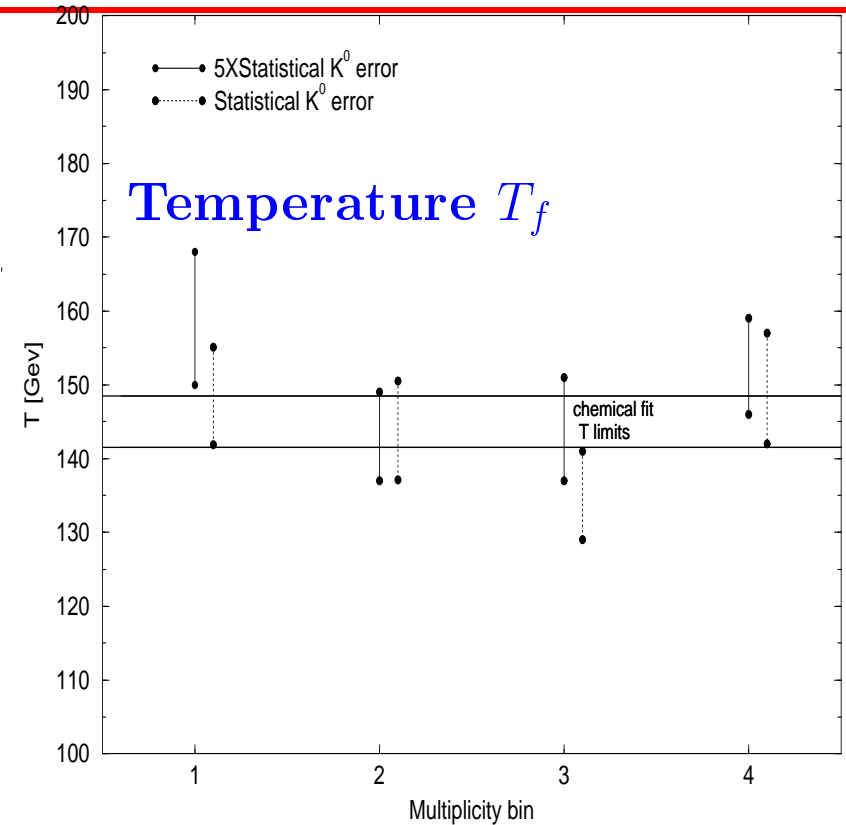
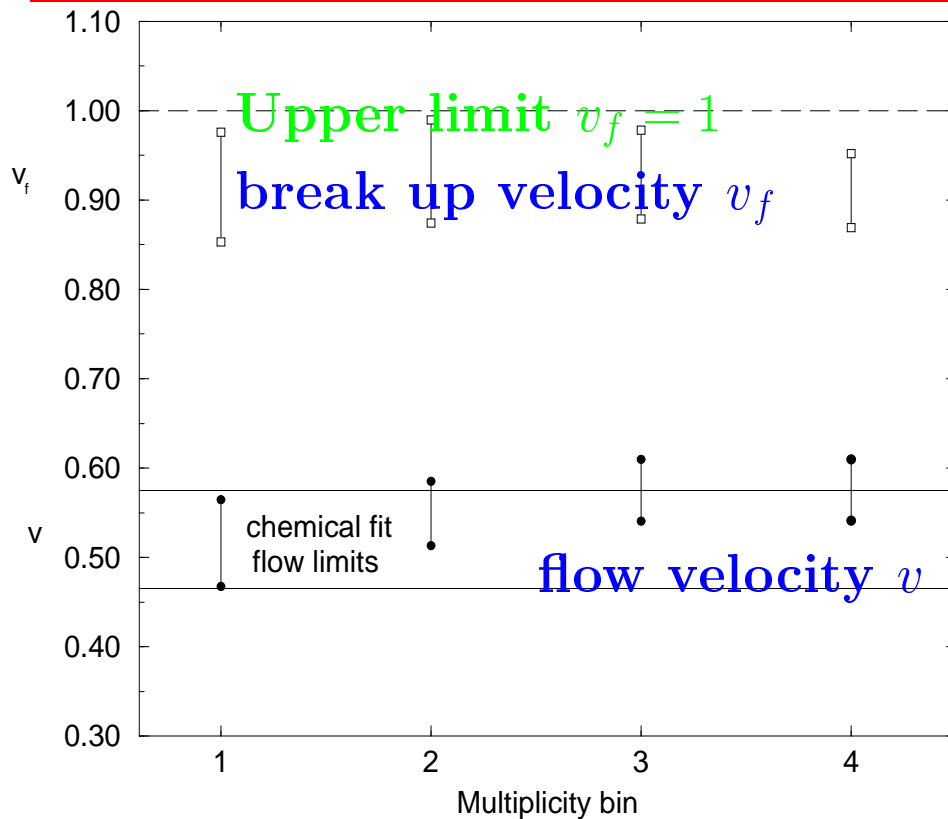


$\partial t_f / \partial r_f = 1/v_f$ on RIGHT



regular experimental stat. K^0 error.

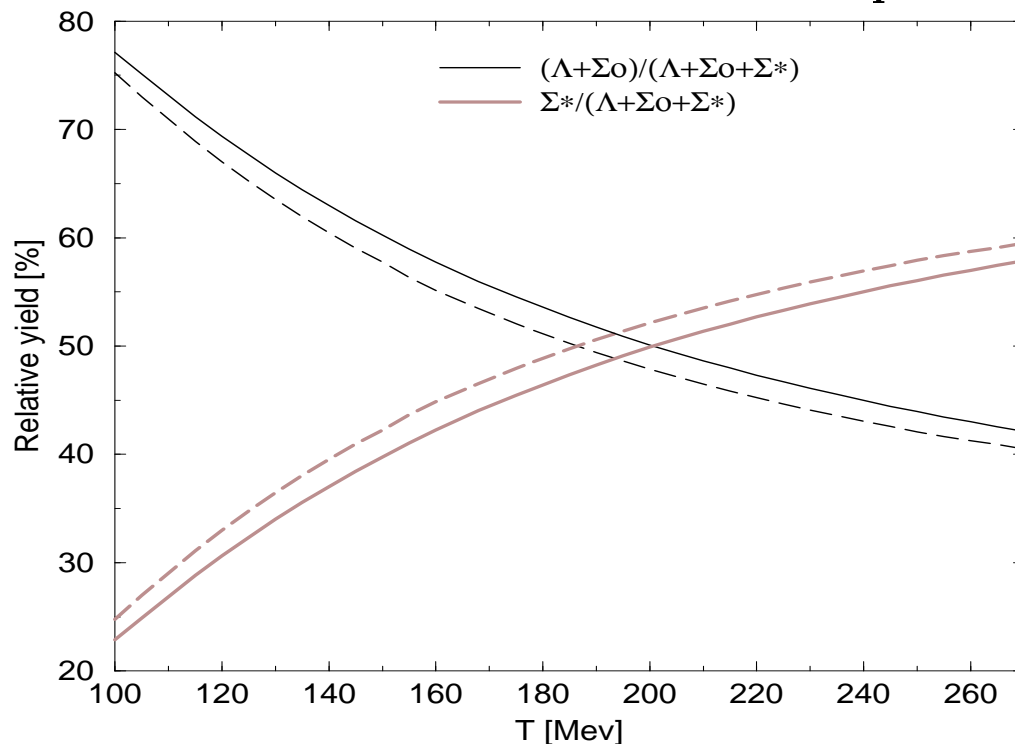
Pb-Pb 158 A GeV CHEMICAL AND THERMAL FREEZE-OUT T, v AGREE



5 different collision centrality bins. We note flow velocity increase (with errors) with increasing size (centrality). Aside of this, there is no indication of a significant or systematic change of T, v, v_f with centrality, e.g. new state of matter is formed in all 4 centrality bins ($A > 100$). It will be interesting to see if the low centrality $A \simeq 50$ studied by experiment WA57 will show different freeze-out properties.

Strange hadron resonances PROBE sudden hadronization

direct experimental measurement!



$\Sigma^*(1385) \rightarrow \Lambda + \pi$ resonance decay contributes significantly to Λ yield. The decay width of $\Gamma_{\Sigma^*} = 35 \text{ MeV} = 1/(5.6 \text{ fm})$ assures that some decays occur within, and some outside the hadron matter – those within matter would be practically all unreconstructable. Candidates for study $\Gamma_{\Lambda(1520)} = 15.6 \text{ MeV} = 1/(12.6 \text{ fm})$; $\Gamma_{K^*(892)} = 50 \text{ MeV} = 1/(4 \text{ fm})$ and $\Gamma_{\Sigma^*(1385)} = 35 \text{ MeV} = 1/(5.6 \text{ fm})$. Complication: quenching.

RESONANCE QUENCHING

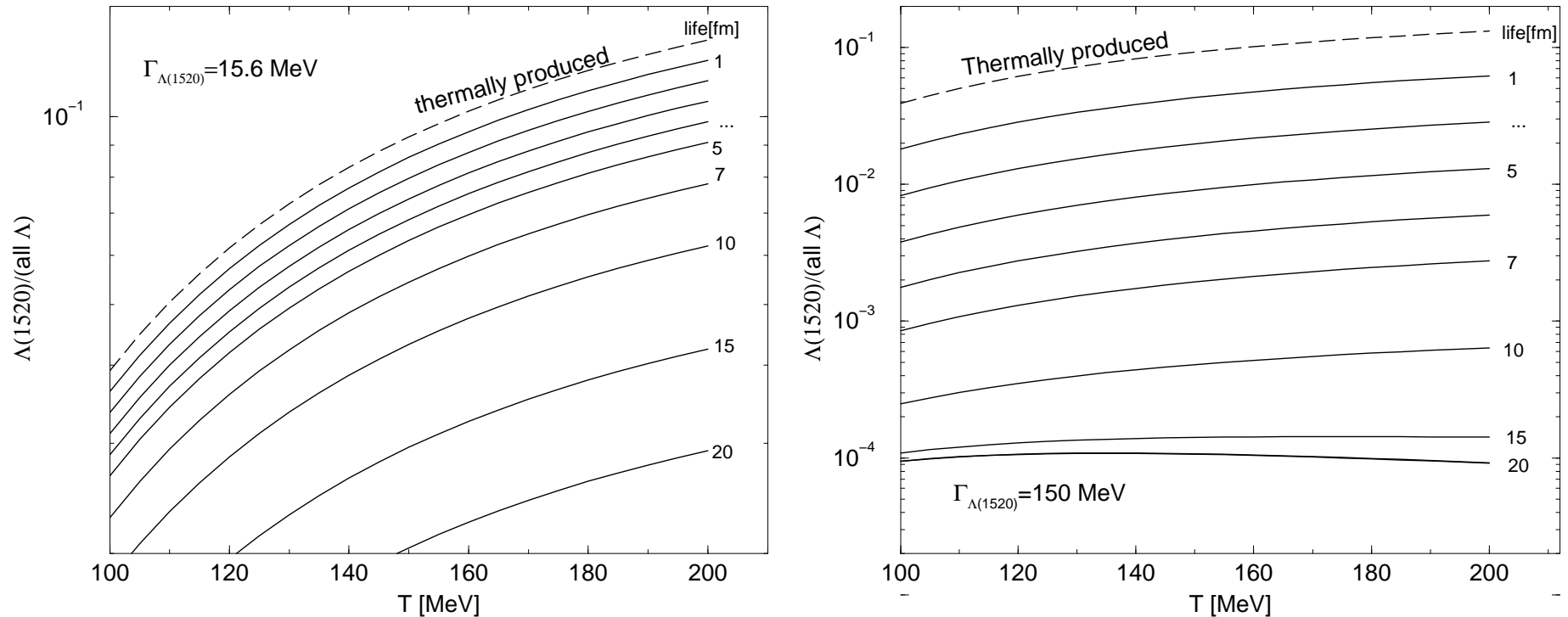
IF DECAY IN FREE SPACE IS BLOCKED BY SUPERSELECTION RULE, QUENCHING IS EFFECTIVE! A possible explanation of $\Lambda(1520)$ suppression reported by NA49.

$$\pi + \Lambda(1520) \rightarrow \Sigma^* \rightarrow \pi + \Lambda,$$

Possible since $\Gamma_{\Lambda(1520)}$ is small due to need for angular $L = 2$ partial wave in its decay. Collisional widening of a metastable state is a familiar phenomenon explored in several areas of physics. The decay of the $\phi(s\bar{s})$ has been the 'usual suspect' in search for such a quenching, given the proximity of the $K\bar{K}$ mass threshold. NOTE: reconstructed line shape will always have the natural width, since rapid in-matter-decay products rescatter not allowing $\Lambda(1520)$ reconstruction!

Try to compare with experiment aside of natural width also a width which is usual for hadronic resonances, $\Gamma_{\Lambda(1520)} = 150 \text{ MeV}$.

Yields as function of t and T

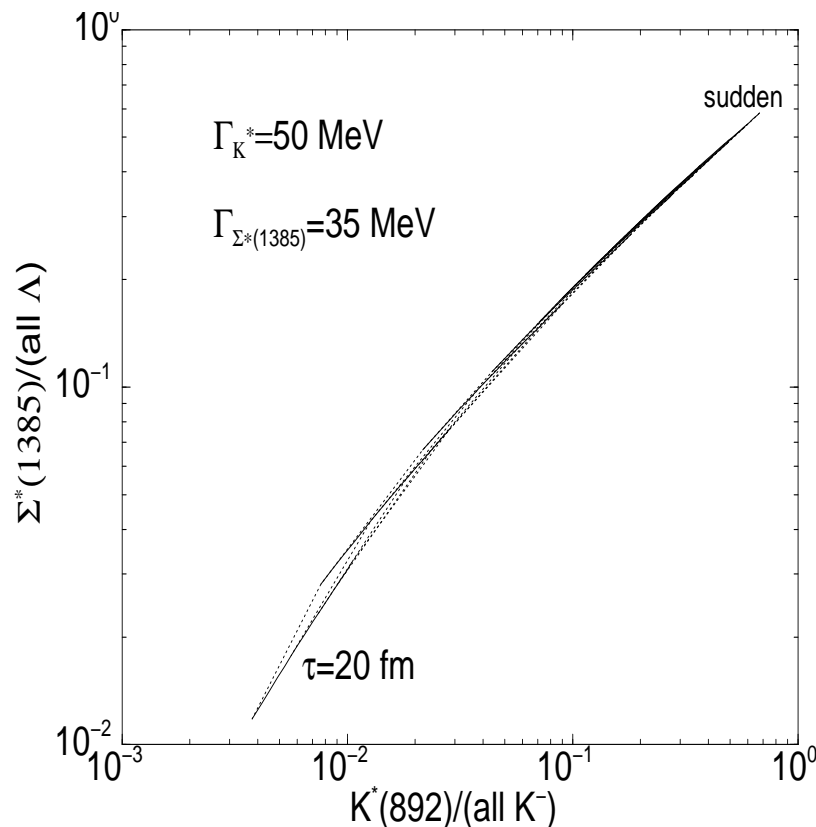
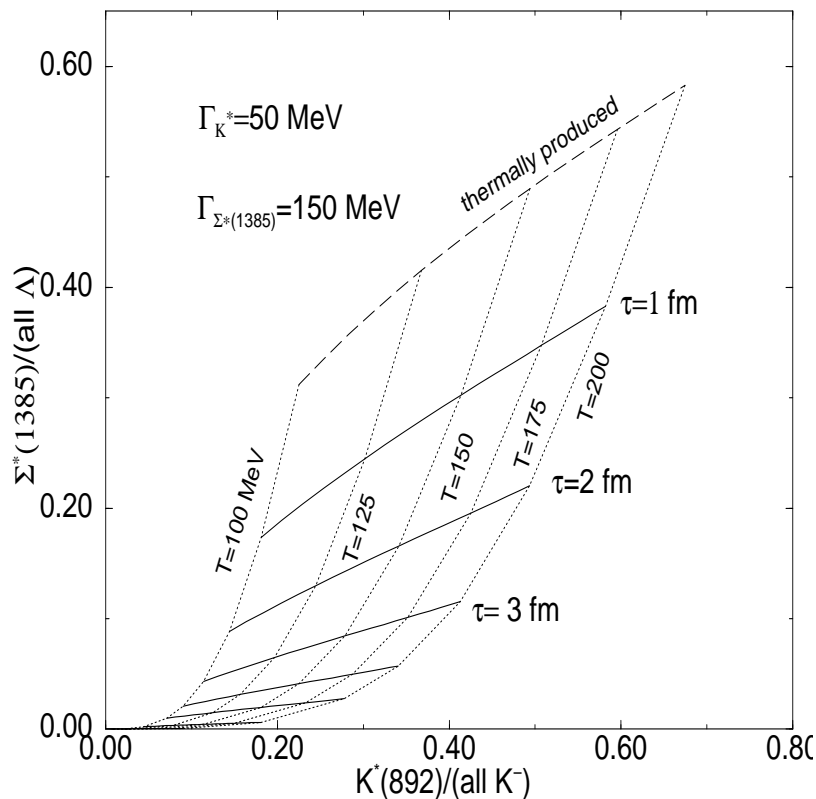


Relative $\Lambda(1520)/(\text{all } \Lambda)$ yield as function of freeze-out temperature T . Dashed - thermal yield, solid lines: observable yield for evolution lasting the time shown (1...20 fm) in an opaque medium.

LEFT: natural $\Gamma_{\Lambda(1520)} = 15.6 \text{ MeV}$, **RIGHT:** quenched $\Gamma_{\Lambda(1520)}^* = 150 \text{ MeV}$.
NA49 measures in $pp \simeq 0.11 \pm 0.02$, in $\text{Pb-Pb} \simeq 0.025 \pm 0.008$.

HOW TO FIX value of Γ^* ?

Evaluate TWO resonances; EXAMPLE

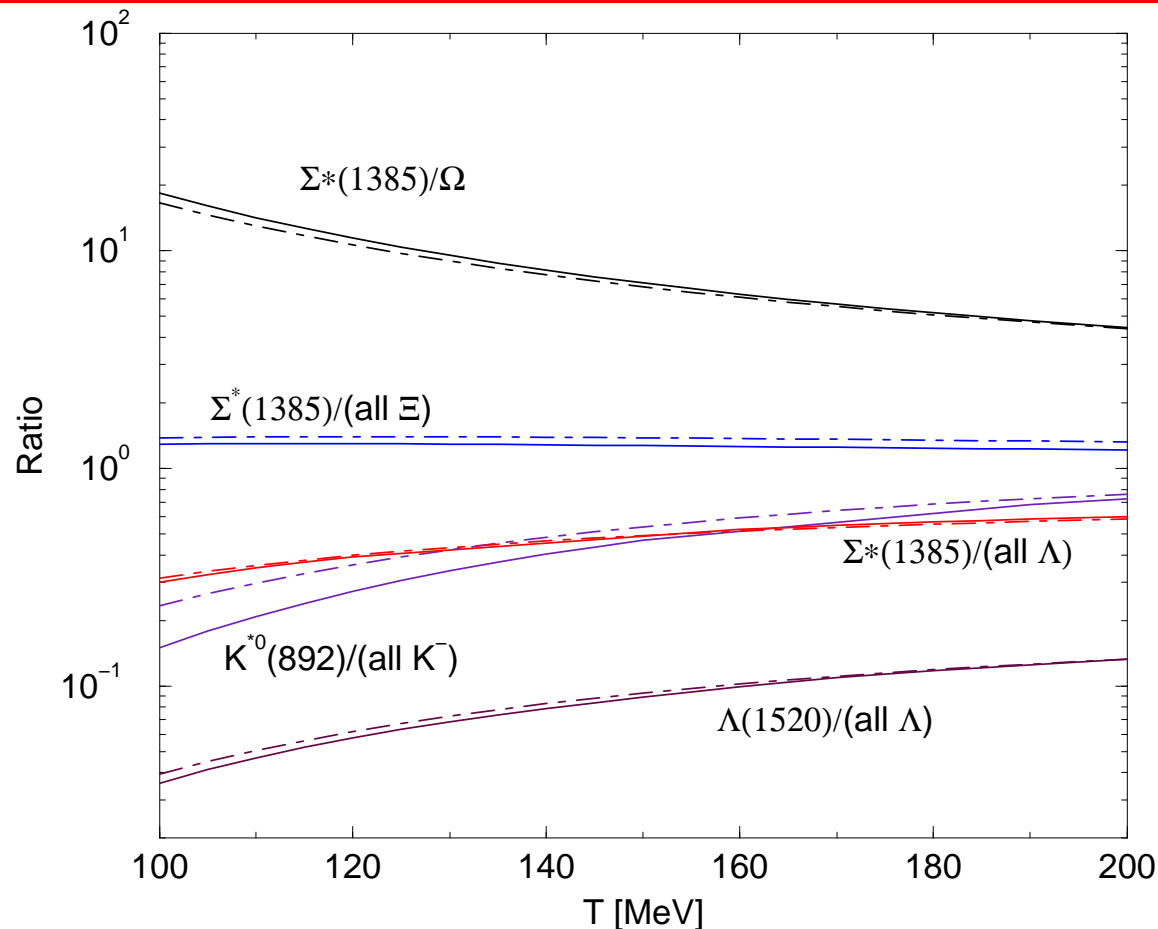


Dependence of the combined $\Sigma^*/(\text{all } \Lambda)$ with $K^*(892)/(\text{all } K^-)$ signals on the chemical freeze-out temperature and HG phase lifetime.

LEFT: quenched $\Gamma_{\Sigma^*} = 150$

RIGHT natural widths

Method Sensitivity and Practicability – RELATIVE RESONANCE CONTRIBUTIONS



Temperature dependence: Solid line all rapidity, dashed lines central rapidity $\Delta y = \pm 0.5$. Note Σ^* is more abundant than all Ξ .

Strangeness at RHIC-130A GeV

$$\frac{dN_{K^+}}{dy}\Big|_{y=0} = 35 \pm 10\%, \quad \frac{dN_{K^-}}{dy}\Big|_{y=0} = 30 \pm 10\%, \quad \frac{d\bar{s}}{dy}\Big|_{y=0} > 85 \pm 10\%.$$

Total strangeness (\bar{s}) yield depends on unmeasured hyperons. Model calculations suggest more than 20%. Hence the last result above.

Compare this to

$$\frac{d\pi^+}{dy} \simeq \frac{d\pi^-}{dy} \simeq 235$$

Calculations suggest that $\bar{s}/b \simeq 8$ (11–12 times greater than at 17A GeV SPS Pb–Pb).

EXTREMELY difficult to imagine that among three quarks which coalesce to make a baryon there is no strange quark! Hence we predicted **HYPERON DOMINANCE** of baryon/antibaryon yields.

Because the hyperon decays are contaminating in a dominant way baryon multiplicity, and K^* yields are **AFTER** hadronization deductability attenuation, **STUDY OF RHIC MULTIPLICITIES AND INTERPRETATION** of particle ratios in terms of statistical parameters is not possible yet in the same way we did this for SPS. We can take a first glimpse:→

Look at STAR data presented at QM2001:

- 1) from $\bar{p}/p = 0.6 \pm 0.02 = \lambda_q^{-6}$ it follows $\lambda_q = 1.09$. $\lambda_s = 1$ in any FIT STRATEGY!
- 2) and hence $\mu_B = 38\text{MeV}$ (18% of SPS value) at $T = 150$ MeV.
- 3) The ratios $\bar{\Lambda}/\Lambda = 0.73 \pm 0.03 = \lambda_s^{-2}\lambda_q^{-4}$ and $\bar{\Xi}/\Xi = 0.82 \pm 0.08 = \lambda_s^{-2}\lambda_q^{-4}$ are consistent within 1.5% with $\lambda_s = 1$, value expected for sudden hadronization.
- 4) $K^+/K^- = 0.88 \pm 0.06$ is also consistent within error with $\lambda_q = 1.089$.
- 5) On the other hand the ratio $K^*/\bar{K}^* \simeq 1$ is inconsistent with this analysis and K/\bar{K} . This suggests that K^*, \bar{K}^* yields are influenced by 'in hadronization' decay product rescattering in a asymmetric way and thus:
- 6) K^*, \bar{K}^* MAY NOT be used to fix T using the ratios K^*/h^- and \bar{K}^*/h^- .
- 7) Ratio $\bar{p}/\pi = 8\%$ cannot be used to fix T since yield of \bar{p} required large hyperon correction.
- 8) The ratio K^-/π^- DOES NOT SUFFICE TO FIX temperature: we need at least 3 reliable yield ratios as we must also fix γ_q, γ_s : $K^-/\pi^- = 15\% = f(T)\gamma_s/\gamma_d$.

First result on chemical potentials, BUT T and γ_q, γ_s cannot yet be fixed.