Relativistický seminář
Ústavu teoretické fyziky

Seminář se koná v úterý ve 13:10 v posluchárně ÚTF MFF UK v 10. patře katedrové budovy v Trójí, V Holešovičkách 2, Praha 8

6. března 2018

Extreme light physics frontier
Prof. Johann Rafelski
Department of Physics, University of Arizona, Tuscon

(seminář v angličtině)
New foundational physics opportunities arising in the context of extreme light technologies being implemented at ELI. I will show how particle dynamics at the extreme acceleration condition relate to the understanding of vacuum structure in the presence of extreme EM fields. I will argue that we will be able to connect theoretical ideas about radiation-reaction improved forces to feasible experiments. I will describe efforts to improve classical relativistic dynamics both in radiation reaction and magnetic moment regime.
Extreme Light Physics Frontier

- Intro: Extreme Light and Critical Fields/Acceleration
- Regime of critical acceleration: Light+Heavy Ions
- Critical acceleration=critical fields, pair production
- Quantum vacuum =Einstein aether+Mach princip.
- More on quantum vacuum structure
- Incompleteness in EM Theory
- Magnetic force
- Vacuum friction: radiation reaction force
- Concluding remarks
ELI will comprise 4 branches:

- **Attosecond Laser Science**, which will capitalize on new regimes of time resolution (*ELI-ALPS, Szeged, HU*)

- **High-Energy Beam Facility**, responsible for development and application of ultra-short pulses of high-energy particles and radiation stemming from relativistic and later ultrarelativistic interaction (*ELI-Beamlines, Prague, CZ*)

- **Nuclear Physics Facility** with ultra-intense lasers and brilliant gamma beams (up to 19 MeV) enabling also brilliant neutron beam generation with a largely controlled variety of energies (*ELI-NP, Magurele, RO*)

- **Ultra-High-Field Science** centred on direct physics of the unprecedented laser field strength (*ELI 4, to be decided*)
Critical Fields=

Critical Acceleration

An electron in presence of the critical ‘Schwinger’ (Vacuum Instability) field strength of magnitude:

$$E_s = \frac{m_e^2 c^3}{e\hbar} = 1.323 \times 10^{18} \text{ V/m}$$

is subject to critical natural unit =1 acceleration:

$$a_c = \frac{m_e c^3}{\hbar} \rightarrow 2.331 \times 10^{29} \text{ m/s}^2$$

Truly dimensionless unit acceleration arises when we introduce specific acceleration

$$\Xi = \frac{a_c}{mc^2} = \frac{c}{\hbar}$$

Specific unit acceleration arises in Newton gravity at Planck length distance: $\Xi_G \equiv G/L_p^2 = c/\hbar$ at $L_p = \sqrt{\hbar G/c}$.

In the presence of sufficiently strong electric field $E_s$ by virtue of the equivalence principle, electrons are subject to Planck ‘critical’ force.
Planck units

\[ \frac{\hbar}{k_B} = a = 0.4818 \times 10^{-10} \text{[sec \times Celsiusgrad]} \]
\[ \hbar = b = 6.885 \times 10^{-27} \left[ \frac{\text{cm}^2 \text{g}}{\text{sec}} \right] \]
\[ c = c = 3.00 \times 10^{10} \left[ \frac{\text{cm}}{\text{sec}} \right] \]
\[ G = f = 6.685 \times 10^{-8} \left[ \frac{\text{cm}^3}{\text{gr sec}^2} \right] \]

Wählt man nun die «natürlichen Einheiten» so, dass in dem neuen Maßsystem jede der vorstehenden vier Constanten den Werth 1 annimmt, so erhält man als Einheit der Länge die Größe:

\[ \sqrt{2\pi} L_{\text{Pl}} = V_{\hbar \phi} = 4.13 \times 10^{-33} \text{cm} \]
als Einheit der Masse:

\[ \sqrt{2\pi} M_{\text{Pl}} = V_{\hbar \phi} = 5.56 \times 10^{-8} \text{gr} \]
als Einheit der Zeit:

\[ \sqrt{2\pi} t_{\text{Pl}} = V_{\hbar \phi} = 1.38 \times 10^{-43} \text{sec} \]
als Einheit der Temperatur:

\[ \sqrt{2\pi} T_{\text{Pl}} = a V_{\hbar \phi} = 3.50 \times 10^{32} \text{Cels} \]

Diese Größen behalten ihre natürliche Bedeutung so lange bei, als die Gesetze der Gravitation, der Lichtfortpflanzung im Vacuum und die beiden Hauptsätze der Wärmetheorie in Gültigkeit bleiben, sie müssen also, von den verschiedensten Intelligenzen nach den verschiedensten Methoden gemessen, sich immer wieder als die nämlichen ergeben.

"These scales retain their natural meaning as long as the law of gravitation, the velocity of light in vacuum and the central equations of thermodynamics remain valid, and therefore they must always arise, among different intelligences employing different means of measuring." M. Planck, "Über irreversible Strahlungsvorgänge." Sitzungsberichte der Königlich Preußischen Akademie der Wissenschaften zu Berlin 5, 440-480 (1899), (last page)
Current experiments in the regime of critical acceleration:

a) Electron-laser pulse collisions

b) Relativistic nuclear (heavy ion) collisions
Probing super-critical (Planck) acceleration

\[ a_c = 1 (\rightarrow m_e c^3 / h = 2.331 \times 10^{29} \text{m/s}^2) \]

Plan A: Directly laser accelerate electrons from rest, requires Schwinger scale field and may not be realizable – backreaction and far beyond today’s laser pulse intensity technology.

Plan B: Ultra-relativistic Lorentz-boost: we collide counter-propagating electron and laser pulse.
SLAC’95 experiment below critical acceleration

\[ p_e^0 = 46.6 \text{ GeV}; \text{ in } 1996/7 \ a_0 = 0.4, \quad \left| \frac{du^\alpha}{d\tau} \right| = 0.073 [m_e] \text{ (Peak)} \]

Multi-photon processes observed:
- Nonlinear Compton scattering
- Breit-Wheeler electron-positron pairs

\[ \text{pair spectrometer} \]

Puls Lorentz Transform (LT)

Relativistic electron-laser pulse collision

\[ u^\beta = \gamma(1, \vec{v}) \rightarrow \text{In electron’s rest frame: } u'_\beta = (1, \vec{0}) \]

Doppler shift:

\[ \omega' = \gamma(1 + \vec{n} \cdot \vec{v}) \omega \]

Unit acceleration condition:

\[ a_0 \frac{\omega'}{m_e} \approx 2 \gamma a_0 \frac{\omega}{m_e} \rightarrow 1 \]
Example: Electron de-acceleration by a pulse

Lorentz invariant acceleration $\sqrt{-\dot{u}^\alpha \dot{u}_\alpha} \ [m_e]$ function of time

Red: solution of Lorentz equation

Collision between a circularly polarized square plane wave with $a_0 = 100$ and initial $E_e = 0.5$ GeV, $\gamma = 1,000$ electron,

Radiation reaction regime

Deviations from Lorentz force impact significantly Lorentz dynamics in dark shaded area of the $\gamma, a_0$ plane
Melting the QCD quantum vacuum

Nuclear Collisions at Relativistic energy $E \gg MC^2$

<table>
<thead>
<tr>
<th>Big-Bang</th>
<th>Micro-Bang</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\tau \approx 10\mu s$</td>
<td>$\tau \approx 4 \times 10^{-23}s$</td>
</tr>
<tr>
<td>$N_b / N \approx 10^{-10}$</td>
<td>$N_b / N \approx 0.1$</td>
</tr>
</tbody>
</table>

Charles U 6.3.18
Johann Rafelski, Arizona
Critical acceleration probably achieved at RHIC

Two nuclei smashed into each other from two sides: components ‘partons’ can be stopped in CM frame within $\Delta \tau \approx 1$ fm/c. Tracks show multitude of particles produced, as observed at RHIC (BNL).

- The acceleration $a$ achieved to stop some/any of the components of the colliding nuclei in CM: $a \approx \frac{\Delta y}{M_i \Delta \tau}$. Full stopping: $\Delta y_{\text{SPS}} = 2.9$, and $\Delta y_{\text{RHIC}} = 5.4$. Considering constituent quark masses $M_i \approx M_N/3 \approx 310$ MeV we need $\Delta \tau_{\text{SPS}} < 1.8$ fm/c and $\Delta \tau_{\text{RHIC}} < 3.4$ fm/c to exceed $a_c$.
Color confinement due to gluon fluctuations

- QCD induces chromo-electric and chromo-magnetic fields throughout space-time – the vacuum is in its lowest energy state, yet it is strongly structured. Fields must vanish exactly everywhere \( \langle H \rangle = 0 \)

- This is an actual computation of the four-d (time +3-dimensions) structure of the gluon-field configuration. The volume of the box is 2.4 by 2.4 by 3.6 fm, big enough to hold a couple of protons.

- Derek B. Leinweber’s group (U Adelaide)

Numerical Method used: lattice in space time

Square of fields does not average out: “condensates

\[
\langle \overline{q}q \rangle = (235 \text{ MeV})^3, \left\langle \frac{\alpha_s}{\pi} G_{\mu\nu} G^{\mu\nu} \right\rangle = (335 \text{ MeV})^4
\]
Melt the quantum vacuum

- $T < \sim 10^3 \, \text{K} \implies$ molecules intact
  $T > \sim 10^3 \, \text{K} \ (0.1 \, \text{eV}) \implies$ molecular dissociation

- $T < \sim 10^4 \, \text{K} \implies$ atoms intact
  $T > \sim 10^4 \, \text{K} \ (1 \, \text{eV}) \implies$ atomic ionization, plasma formation

- $T < \sim 10^9 \, \text{K} \implies$ nuclei intact
  $T > \sim 10^9 \, \text{K} \ (0.1 \, \text{MeV}) \implies$ nuclear reactions

- $T < \sim 10^{12} \, \text{K} \implies$ protons intact
  $T > \sim 10^{12} \, \text{K} \ (160 \, \text{MeV}) \implies$ vacuum melts, quarks free

- $T < \sim 10^{15} \, \text{K} \implies$ electromagnetic and weak interactions separate
  $T > \sim 10^{15} \, \text{K} \ (160 \, \text{GeV}) \implies$ Higgs vacuum melts, all quarks massless
Addvert of anothe talk: Strangeness Signature of QGP
REINTERPRETATION Rel. Quantum Physics: Critical Acceleration=Critical Fields
Klein's non-paradox

The Dirac equation uses energy, mass and momentum of special relativity \( E^2 = p^2 c^2 + m^2 c^4 \), taking root we find in quantum physics two energy (particle) bands.

Relativistic Dirac quantum physics predicts antimatter and allows formation of pairs of particles and antiparticles.

The relativistic gap in energy reminiscent of insulators, where conductive band is above the valance (occupied) electron band.
Pair production in constant fields

The sparking of the QED dielectric

O. Klein, Sauter, Euler

Effect large for Field

$$E_s = 1.3 \times 10^{16} \text{ V/cm}$$

*Tomorrow:* In laser focus this corresponds to $$I_s = 2.3 \times 10^{29} \text{ W/cm}^2$$

Probability of vacuum pair production can be evaluated in WKB description of barrier tunneling: All E-fields are unstable and can decay to particles – footnoted by Heisenberg around 1935, added into Schwinger's article as a visibly after finish-point.
Seeking tests: positrons from (quasi-)superheavy elementes 1971-91

(quasi)Atoms beyond $Z \simeq 100$

Single Particle Dirac Equation

$$(\bar{\alpha} \cdot i \nabla + \beta m + V(r)) \Psi_n(r) = E_n \Psi_n(r)$$

$V(r) = \begin{cases} \frac{-Z\alpha}{r} & r > R_N \\ \frac{-3Z\alpha}{2R_N} + \frac{r^2 Z\alpha}{2R_N^3} & r < R_N \end{cases}$

Supercritical fields

The bound states drawn from one continuum move as function of $Z$ across into the other continuum. Mix-up of particle/antiparticle states


Decay of the Vacuum

Undercritical

Overcritical $+ mc^2$

- $mc^2$

If diving state ‘empty’ vacuum decays

$|Q = 0\rangle \rightarrow |Q = e\rangle + e^+$ by positron state occupied by an electron, ‘smooth’ transition of charge distribution
Experimental Realization: Heavy Ion collision
Next:

Quantum Vacuum=Einstein aether (what?)
this provides us with a method to resolve
Mach's dilemma: how to know we are accelerated
Inertia & Mach’s Principle

Measurement of (strong) acceleration requires a reference frame: what was once the set of fixed stars in the sky is today CMB photon freeze-out reference frame. To be consistent with special relativity: all inertial observers with respect to CMB form an equivalence class, we measure acceleration with reference to the CMB inertial frame.

In Einstein’s gravity reference frame provided by metric. However, there is no “acceleration”, a dust of gravitating particles is in free fall. Only in presence of a rigid body created by quantum physics combined with EM force, Mach’s principle a concern, and we are lead to remember the “aether”.

... with the new theory of electrodynamics we are rather forced to have an aether. – P.A.M. Dirac, ‘Is There an Aether?’, Nature, v.168, 1951, p.906.
The word aether in Homeric Greek means “pure, fresh air” or “clear sky”, pure essence where the gods lived and which they breathed. The aether was believed in ancient and medieval science to be the substance that filled the region of the universe above the terrestrial sphere. Aristotle imposed aether as a fifth element filling all space. Aether was later called quintessence (from quinta essentia, "fifth element"). The "luminiferous aether" (light carrying aether) is the “substance” believed by Maxwell, Larmor, Lorentz to permeate all the Universe. Einstein flips on the topic, introduces relativistic aether 1920.
Aether returns 1919/20

General Relativity and Cosmology: gravity as space-time geometry, time has a beginning.
Gravity metric is the new aether.

**Einstein 1920:** “But this aether may not be thought of as endowed with the quality characteristic of ponderable media, as consisting of parts which may be tracked through time. The idea of motion may not be applied to it.”
How can the laws of physics be known in all Universe?

“Recapitulating, we may say that according to the general theory of relativity space is endowed with physical qualities; in this sense, therefore, there exists an aether. But this aether may not be thought of as endowed with the quality characteristic of ponderable media, as consisting of parts which may be tracked through time. The idea of motion may not be applied to it.

“According to the general theory of relativity space without aether is unthinkable; for in such space there not only would be no propagation of light, but also no possibility of existence for standards of space and time (measuring-rods and clocks), nor therefore any space-time intervals in the physical sense.”

TODAY: The laws of physics are encoded in quantum vacuum structure.
A few decades later:

Quantum vacuum structure
Virtual Pairs: The vacuum is a dielectric medium: a charge is screened by particle-hole (pair) excitations. In Feynman language the real photon is decomposed into a bare photon and a photon turning into a “virtual” pair. The result: renormalized electron charge smaller than bare, Coulomb interaction stronger (0.4% effect).

This effect has been studied in depth in atomic physics, is of particular relevance for exotic atoms where a heavy charged particle replaces an electron.
Matter Influences Vacuum

Photons fluctuations altered by matter, Casimir effect can be measured:

Attractive force between two adjacent metal plates (Casimir force, 1948)

\[ F = \frac{\pi^2 \hbar c}{240L^4} A \]

More fluctuations outside the plates compared to the space between: outside pressure, plates attract

NOTE: Each ‘elementary’ particle, each interaction adds a new element to vacuum structure.
A “naive” vacuum structure model of quark confinement in hadrons

Quarks live inside a domain where the (perturbative) vacuum is without gluon fluctuations. This outside structure wants to enter, but is kept away by quarks trying to escape.

- The model assumes that the energy density $E/V=0$ of the true vacuum is lower than the inside of a hadron.
Color confinement due to gluon fluctuations

- QCD induces chromo-electric and chromo-magnetic fields throughout space-time – the vacuum is in its lowest energy state, yet it is strongly structured. Fields must vanish exactly everywhere \( \langle H \rangle = 0 \)

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\]
TODAY: Origin of Forces and Nature of Mass, Stability of Matter

- “Elementary” masses are generated by the vacuum. Two dominant mechanisms:

  - Higgs vacuum: $<H> = 246 \text{ GeV}$; scale of mass for W, Z; contributes to matter particle mass, all of heavy quark mass

  - QCD vacuum latent heat at the level of $<EV_p> = 0.3 \text{ GeV} =$: nuclear mass scale, quarks get mass and are confined.

$$m_e c^2 = 0.511 \text{MeV} \quad m_N c^2 = 0.940 \text{GeV}$$

Units are G=giga, M=mega e=electron charge, V=Volt,
What signals our present theory of essentially “inertial motion” wanting?
The inertial motion defines mass.
Accelerated motion requires introduction of Vacuum friction

“Holy Grail: Lorentz Force”
Incomplete in two independent ways:
a) Magnetic Dipole Force
b) Radiation Reaction Force

Both hard to accommodate by action principle:
Evidence that new theoretical ideas will be needed
Magnetic Force
How magnetic force acts on charged subatomic particles near the speed of light

Current textbooks often refer to the Lorentz-Maxwell force governed by the electric charge. But they rarely refer to the extension of that theory required to explain the magnetic force on a point particle. For elementary particles, such as muons or neutrinos, the magnetic force applied to such charges is unique and immutable. However, unlike the electric charge, the magnetic force strength is not quantised. For the magnetic force to act on them, the magnetic field has to be inhomogeneous. Hence this force is more difficult to understand in the context of particles whose speed is near the speed of light. Moreover, our understanding of how a point-particle carrying a charge moves in presence of an inhomogenous magnetic field relied until now on two theories that were believed to differ. The first stems from William Gilbert’s study of elementary magnetism in 16th century, while the second relies on André-Marie Ampère electric currents. In a new study just published in *EPJ C*, ....
Relativistic dynamics of point magnetic moment
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Department of Physics, The University of Arizona, Tucson, AZ 85721,

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Abstract The covariant motion of a classical point particle with magnetic moment in the presence of (external) electromagnetic fields is revisited. We are interested in understanding extensions to the Lorentz force involving point particle magnetic moment (Stern–Gerlach force) and how the spin precession dynamics is modified for consistency. We introduce spin as a classical particle property inherent to Poincaré symmetry of space-time. We propose a covariant formulation of the magnetic force based on a ‘magnetic’ 4-potential and show how the point particle magnetic moment

The magnetic field and magnetic moment due to natural magnetic dipoles (left), or an electric current (right). Either generates the same field profile.

1. The magnetic moment $\mu$ has an interaction energy with a magnetic field $B$

$$E_m = -\mu \cdot B. \quad (1)$$

The corresponding Stern–Gerlach force $F_{SG}$ has been written in two formats

$$F_{SG} = \begin{cases} \nabla (\mu \cdot B), & \text{Amperian Model}, \\ (\mu \cdot \nabla) B, & \text{Gilbertian Model}. \end{cases} \quad (2)$$
Relativistic ‘magnetic potential’

Since \( E_{\text{mag}} = -\mu \cdot \mathbf{B} \equiv U_{\text{mag}}^0 \) In the rest frame of the particle

\[
U_{\text{mag}}^0 = B^0 c d = -\mu \cdot \mathbf{B}, \quad s \ dc = \mu
\]

Need magnetic ‘charge’ \( d \)

We look at a magnetic 4-potential \( B^\mu \) akin to e-4-potential \( A^\mu \)

\[
B_\mu \equiv F^*_\mu\nu S^\nu, \quad F^*_\mu\nu \equiv \frac{1}{2} \epsilon_{\mu\nu\alpha\beta} F^{\alpha\beta}, \quad F^{\mu\nu} \equiv \partial^\mu A^\nu - \partial^\nu A^\mu
\]

since \( s_\mu \) is axial, \( B^\mu \) is a polar 4-vector.

\( B^\mu \) generates additional magnetic force

\[
m \frac{du^\mu}{d\tau} \equiv F^\mu_{\text{ASG}} = (e F^{\mu\nu} + G^{\mu\nu} d) u_\nu, \quad G^{\mu\nu} \equiv \partial^\mu B^\nu - \partial^\nu B^\mu.
\]
Equivalence of point particle magnetic moment forces

Based on this we can write two equivalent generalizations of the Lorentz force

\[ F^\mu = F^\mu_{\text{ASG}} = eF^{\mu\nu}u_\nu - u \cdot \partial F^{* \mu\nu} s_\nu \, d + \partial^\mu (u \cdot F^* \cdot s \, d) \]
\[ F^\mu = F^\mu_{\text{GSG}} = (eF^{\mu\nu} - s \cdot \partial F^{* \mu\nu} d) u_\nu - \mu_0 j^\gamma \epsilon_{\gamma\alpha\beta\nu} u^\alpha s^\beta g^{\nu\mu} \, d \]

\[ \nabla (\mu \cdot \mathbf{B}) - (\mu \cdot \nabla) \mathbf{B} = \mu \times (\nabla \times \mathbf{B}) \] with this we obtain

**In rest frame**

\[ 0 = [F_{\text{ASG}} - F_{\text{GSG}}]_{RF} \]
\[ = \mu \times \left( -\frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t} + \nabla \times \mathbf{B} - \mu_0 j \right) = 0 . \]

We recognize Maxwell equation in parenthesis
Schwinger shows how the TMBT spin dynamics relates to EM force: given $u \cdot s = 0$ he takes proper time $\tau$ derivative $\dot{u} \cdot s + u \cdot \dot{s} = 0$ and substituting force for $\dot{u}$ for the case of Lorentz dynamics he argues:

$$u_\mu \left( \frac{d s^\mu}{d \tau} - \frac{e}{m} F^{\mu \nu} s_\nu \right) = 0.$$ 

The general solution satisfying this equation is

$$\frac{d s^\mu}{d \tau} = \frac{e}{m} F^{\mu \nu} s_\nu + \frac{\tilde{a} e}{m} \left( F^{\mu \nu} s_\nu - \frac{u_\mu}{c^2} (u \cdot F \cdot s) \right)$$

We repeat the same for our generalized Lorentz force: each component $F^{\mu \nu}$ and $G^{\mu \nu}$ induces two independent integration constants ($\tilde{a}$ and $\tilde{b}$ below)
Radiation Reaction and Vacuum Friction
Strong Field Unsolved Problem
Radiation-Acceleration-Reaction

Conventional Lorentz-Electromagnetic force is incomplete: accelerated charged particles can radiate: “radiation friction” instability – some acceleration produces friction slowdown, produces more slowdown etc. Need acceleration that is not negligible to explore the physics of radiation friction. Problem known for 115 years.

Microscopic justification in current theory (LAD)
1) Inertial Force = Lorentz-force with friction - > get world line of particles=source of fields
2) Source of Fields = Maxwell fields - > get fields, and omit radiated fields
3) Fields fix Lorentz force with friction -> go to 1.

So long as the radiated fields are small, we can modify the Lorentz Force to account for radiated field back reaction. The “Lorentz-Abraham-Dirac (LAD)” patch is fundamentally inconsistent, and does not follow from an action principle. Many other patches exist, some modifying inertia, others field part of Lorentz force - it introduces a nonlinear and partially nonlocal Lorentz-type force. No action principle is known.
Conventional SR+Electromagnetic theory is **incomplete**: radiation emitted needs to be incorporated as a back-reaction “patch”:

1) **Inertial Force = Lorentz-force** --> get world line of particles=source of fields
2) **Source of Fields = Maxwell fields** --> get fields, and omit radiated fields
3) **Fields fix Lorentz force** --> go to 1.

So long as radiated fields are small, we can modify the Lorentz Force to account for radiated field back reaction approximately

**Table 29.1 Models of radiation reaction extensions of the Lorentz force**

<table>
<thead>
<tr>
<th>Model</th>
<th>Equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maxwell-Lorentz</td>
<td>$\mu^\mu = eF^{\mu\nu}u_\nu$</td>
</tr>
<tr>
<td>LAD$^{33}$</td>
<td>$\mu^\mu = eF^{\mu\nu}u_\nu + m\tau_0 \left[ g^{\mu\nu} - \frac{u^{\mu}u^{\nu}}{c^2} \right] \tilde{u}_\nu, \quad \tau_0 = \frac{2}{3} \frac{e^2}{4\pi\varepsilon_0 mc^3}$</td>
</tr>
<tr>
<td>Landau-Lifshitz$^{35}$</td>
<td>$\mu^\mu = eF^{\mu\nu}u_\nu + e\tau_0 \left{ u^\nu \partial_\nu F^{\mu\delta}u_\delta + \frac{e}{m} \left( g^{\mu\nu} - \frac{u^{\mu}u^{\nu}}{c^2} \right) F_{\gamma\beta} F_\delta^{\gamma\beta} u_\delta \right}$</td>
</tr>
<tr>
<td>Caldirola$^{36}$</td>
<td>$0 = eF^{\mu\nu}(\tau)u_\nu(\tau) - m \left[ g^{\mu\nu} - \frac{u^{\mu}(\tau)u^{\nu}(\tau)}{c^2} \right] \left{ u_\nu(\tau) - u_\nu(\tau - 2\tau_0) \right} \frac{2\tau_0}{2\tau_0}$</td>
</tr>
</tbody>
</table>
Concluding Comments
To resolve inconsistencies: we need to formulate a NEW “large acceleration” theory of electro-magnetism, comprising Mach’s principle, and challenging understanding of inertia.

THEORY Question: How to achieve that charged particles when accelerated radiate in self-consistent field – and we need EM theory with Mach principle accounted for (gravity, quantum physics=zero acceleration theories)!

EXPERIMENT: strong acceleration required. What is strong: unit acceleration=Heisenberg-Schwinger Field

Is there a limit to how fast we can accelerate electrons to ultra high energy? Example of early Model: Born-Infeld electromagnetism/

Can the empty space remain transparent to a plane wave of arbitrary intensity? And why? **Perfect translational symmetry required.**
High-Energy Beam Facility, responsible for development and application of ultra-short pulses of high-energy particles and radiation stemming from relativistic and later ultrarelativistic interaction.
Summary: A new path to probing space time

The new idea is to collide kJ pulses with themselves or with particles, with light intense enough to crack the vacuum.

On the way we can study nonlinear QED.

Pair $e^+e^-$ production.

EM fields polarize quarks in QCD vacuum.

Should we be able to focus of 5kJ to 10% atom size we reach energy density of QGP. Macroscopic domain of early Universe.

...and if we get that energy into proton sized volume the Higgs vacuum will melt.
(Special) Relativity evolves

Relativity Matters
From Einstein's EMC2 to Laser Particle Acceleration and Quark-Gluon Plasma

Authors: Johann Rafelski

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Text pdf available for free if your library subscribes to Springer Physics
Relativity Matters: From Einstein's EMC2 to Laser Particle Acceleration and Quark-Gluon Plasma
By: Johann Rafelski

Relativity Matters has all the hallmarks of becoming a classic with further editions, and appears to have no counterpart in the literature. This is particularly useful because at present SR has become a basic part not only of particle and space physics, but also of many other branches of physics and technology, such as lasers. The book has 29 chapters organised in 11 parts, which cover topics from the basics of four-vectors, space-time, Lorentz transformations, mass, energy and momentum, to particle collisions and decay, the motion of charged particles, covariance and dynamics.

The first half of the book derives basic consequences of the SR axioms with a minimum of mathematical tools. It concentrates on the explanation of apparently paradoxical results, presenting and refuting counterarguments as well as debunking various incorrect statements in elementary textbooks. This is done by cleverly exploiting the Galilean method of a dialogue between a professor, his assistant and a student, to bring out questions and objections.

The importance of correctly analysing the consequences for extended and accelerating bodies is clearly presented. Among the many

An interesting afterword concluding the book discusses how very strong acceleration becomes a modern limiting factor, beyond which SR in classical physics becomes invalid. The magnitude of the critical accelerations and critical electric and magnetic fields are qualitatively discussed. It also briefly analyses attempts by well-known physicists to sidestep the problems that arise as a consequence.

Relativity Matters is excellent as an undergraduate and graduate textbook, and should be a useful reference for professional physicists and technical engineers. The many non-specialist sections will also be enjoyed by the general, science-interested public.

Johann Rafelski, CERN
All of SR tested but body contraction

Idea: use reflection from relativistic electron mirror

The moving electron cloud mirror is body compressed.

Body contraction experiment. — To accomplish our goal to build a laboratory-sized experiment we consider an ultra-intense ultra-short laser pulse shot at a thin (micron) foil. Such a pulse in its focal point can act as a micron-sized hammer pushing out of the foil an electron cloud accelerated to ultrarelativistic motion with a high value of Lorentz-factor $\gamma_e$. The emerging electron cloud compared to the original foil thickness will be Lorentz-FitzGerald compressed by $\gamma_e$.

A moving electron cloud acts as a relativistic mirror for a low intensity laser light bounce. The capability of the ultrarelativistic mirror to function depends on the electron cloud density; laser light can scatter coherently from a sufficiently high density cloud – what is low and high density is determined by comparing mean electron separation to the light wavelength. Two Lorentz transforms, first into the rest-frame of the mirror and upon reversal of the propagation direction of the light motion, transform back to the laboratory frame.
EXTRA SLIDES
Moving foil-electron cloud: Coherent backscattering

\[ \omega_r = \frac{C + V}{C - V} \omega_0 = \gamma^2 \omega_0 \]
The Higgs vacuum and symmetry breaking

Higgs field in the vacuum makes weak interactions weak and 2nd and 3rd particle generation heavy
Quantum Chromo-Dynamics (QCD): Quark colour field lines confined

Most of the mass of visible matter is due to QCD -
More forces between matter particles

Gravity is an effective force which we do not understand, conflict with quantum physics.

‘Higgs’ vacuum structure breaks the electro-weak symmetry: W, Z turn very massive, weak interactions.

Quantum Chromo-Dynamics (QCD): theory of strong interactions with a confining dynamical vacuum structure.

QCD: a world in which “photons” have a “color magnetic moment”: vacuum consists of a ferromagnetic alignment of glue fluctuations.
A new structured stable local vacuum state

There is localized charge density in the vacuum, not a particle of sharp energy. Formation of the charged vacuum ground state observable by positron emission: which fills any vacancies among ‘dived’ states in the localized domain.

Speed of decay of false vacuum controlled by (Heisenberg-Schwinger) field strength.
Do we live in False vacuum?

“We conclude that there are no credible mechanisms for catastrophic scenarios (with heavy ion collisions at RHIC)” (Jaffe, R.L., Busza, W., Sandweiss, J., and Wilczek, F, 2000, Rev. Mod. Phys. 72, 1125-1140)
Do we live in False vacuum?

Dark Energy: (unlike dark matter) a property of the vacuum indicating we are not in ground state in the Universe (could be the case near to matter).

Can we really proceed to plan experiments and to travel back in time to the beginning of the Universe.
Dynamical Emergence of the Universe into the False Vacuum

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Abstract. We study how the hot Universe evolves and acquires the prevailing vacuum state, demonstrating that in specific conditions which are believed to apply, the Universe becomes frozen into the state with the smallest value of Higgs vacuum field $v = (h)$, even if this is not the state of lowest energy. This supports the false vacuum dark energy $\Lambda$-model. Under several likely hypotheses we determine the temperature in the evolution of the Universe at which two vacua $v_1, v_2$ can swap between being true and false. We evaluate the dynamical surface pressure on domain walls between low and high mass vacua due to the presence of matter and show that the low mass state remains the preferred vacuum of the Universe.

1 Introduction

This work presents relatively simple arguments for why the cosmological evolution selects the vacuum with smallest Higgs VEV $v = (h)$, which, in general, could be and likely is the ‘false’ vacuum. Our argument relies on the Standard Model (SM) minimal coupling $m \to gh$, or similar generalizations in ‘beyond’ SM (BSM), so that the vacuum with the smallest Higgs VEV also has the smallest particle masses. In anticipation of the model with multiple vacua, we call the vacuum state with lowest free energy at temperature $T$ ‘the true vacuum’ and all others ‘the false vacua’. Note that this is a temperature dependent statement: we live today in the false vacuum which as we will show was once the true vacuum.

In the presence of pairs of particles and antiparticles at high temperature the vacuum state with smallest $v$ is energetically preferred, even if it has a huge vacuum energy. This is so because smaller $v$ implies smaller particle masses and hence less energy, and free energy, in the particle distributions. By the time the Universe cools sufficiently for the larger vacuum energy to dominate the smaller particle free energies, the probability of swap to the large mass true vacuum is vanishingly small in general.

Therefore, the Higgs minimum with the lowest value of the Higgs field $v$, and thus not necessarily the lowest value of the effective potential $W(v) = (V(h))$, emerges as the prevalent vacuum in our Universe. The difference, $\rho_{v} = \Delta W$, between the prevalent vacuum state today and the true minimum is a natural candidate to explain the observed dark energy density.

\[
\rho_v = \frac{25.6}{m^4}.
\]
How was matter created?

Matter emerges from quark-gluon plasma

After the Big-Bang the “vacuum” was different till about at 30 μs – expansion cooled the temperature $T$ to a value at which vacuum changed and our matter “froze out”. At that time the density of matter was about $\sim 10^{16} \text{ gm / cm}^3$ (energy density $\sim 10 \text{ GeV / fm}^3$, well above that of the center of neutron stars, that is $\sim 60$ times nuclear energy density), and temperature was $T \sim 160 \text{ MeV}$, that is $\sim 2 \times 10^{12} \text{K}$.