Quantum Vacuum and Strong Fields
Talking Points

Aether of XXI Century = Structured Quantum Vacuum

Dirac and (anti)Matter

Strong Fields: Local Structured Vacuum 1968-86

Back to Strong Fields: Magnetic anomaly (ends page 34)

Quark Confinement a vacuum effect

Vacuum Determines Laws of Physics and The Universe

Critical Fields=Critical Acceleration with Radiation-Reaction

(ends page 61)
Aether of XXI Century=
The Structured Quantum Vacuum
First Ideas about space-time
Four elements and the aether

- The word aether in Homeric Greek means “pure, fresh air” or “clear sky”, pure essence where the gods lived and which they breathed. The aether was believed in ancient and medieval science to be the substance that filled the region of the universe above the terrestrial sphere.

Fire:=energy; Air:=gas phase;
Water:=liquid phase; Earth:=solid phase; Aether:=vacuum
The Scientific Revolution begins: Inertia & Mach’s Principle
How can we know about “acceleration”

Measurement of acceleration requires a universal inertial reference frame: what was once the set of fixed stars in the sky is today CMB photon freeze-out reference frame. All inertial observers with respect to CMB form an “equivalence class”, we measure acceleration with reference to the CMB inertial frame. It is rather clear that the information about who is accelerating must be provided locally and instantaneously. In Einstein’s gravity reference frame provided by metric tensor. However, in GR there is no “acceleration”, a dust of gravitating particles is in free fall. TODAY: The laws of physics are encoded in quantum vacuum structure.

... with the new theory of electrodynamics (QED, jr) we are rather forced to have an aether. – P.A.M. Dirac, ‘Is There an Aether?,’ Nature, v.168, 1951, p.906.
Einstein: Letter to Lorentz 1919: “It would have been more correct if I had limited myself, in my earlier publications, to emphasizing only the non-existence of an aether velocity, instead of arguing the total non-existence of the aether, for I can see that with the word aether we say nothing else than that space has to be viewed as a carrier of physical qualities.”

Ather und die Relativitaetstheorie (Berlin, 1920):

“Recapitulating, we may say that according to the general theory of relativity space is endowed with physical qualities; in this sense, therefore, there exists an aether.”

“According to the general theory of relativity space without aether is unthinkable; for in such space there not only would be no propagation of light, but also no possibility of existence for standards of space and time (measuring-rods and clocks), nor therefore any space-time intervals in the physical sense.”

“But this aether may not be thought of as endowed with the quality characteristic of ponderable media, as consisting of parts which may be tracked through time. The idea of motion may not be applied to it.”
What is new in Quantum Mechanics?

The uncertainty principle of quantum physics

\[ \Delta E \cdot \Delta t \geq \hbar \]

Forbids a truly empty world

The quantum uncertainty challenges the idea of “empty” space free of matter

Vacuum = “ground state” of lowest energy of a physical system

M Planck  N Bohr  L de Broglie  E Schroedinger  W Heisenberg  M Born
Matter Influences Quantum Vacuum

**Photons** fluctuations altered by matter, Casimir effect can be measured:

Attractive force between two adjacent metal plates (Casimir force, 1948)

\[ F = \frac{\pi^2}{240} \frac{\hbar c}{L^4} A \]

More fluctuations outside the plates compared to the space between: outside pressure, plates attract

**NOTE:** Each ‘elementary’ particle, each interaction adds a new “fluctuation” to vacuum structure.
Dirac matters:
Relativity extends the quantum world: Paul Dirac – memorial in St Maurice, VS
Antimatter not yet recognized: Klein's “Paradox”

The Dirac equation uses energy, mass and momentum of special relativity $E^2 = p^2c^2 + m^2c^4$, taking root we find in quantum physics two energy (particle) bands. A potential mixes these states!
Tunneling instability and pair production: Extension of Klein's paradox

Relativistic Dirac quantum physics predicts antimatter and allows formation of pairs of particles and antiparticles.

The relativistic gap in energy reminiscent of insulators, where conductive band is above the valance (occupied) electron band.
Rate of surface pair production in “constant” fields

The sparking of the QED dielectric

Effect large for Field

\[ E_s = 1.323 \times 10^{18} \text{ V/m} \]

Probability of pair production can be evaluated in WKB description of barrier tunneling: All E-fields are unstable and can decay to particles if energy is available and rate is large enough – footnoted by Heisenberg around 1935, in 1950 Schwinger's article as an visibly after finish-point (my idea how this happened: invited by referee=Heisenberg?).
Virtual Pairs: The vacuum is a dielectric medium: a charge is screened by particle-hole (pair) excitations. In Feynman language the real photon is decomposed into a bare photon and a photon turning into a “virtual” pair. The result: renormalized electron charge smaller than bare, Observable Coulomb interaction stronger (0.4%) at distance $1/m$

This effect has been studied in depth in atomic physics, is of particular relevance for exotic atoms where a heavy (muon) charged particle replaces an electron.
Strong Fields
Local Structured Vacuum
The prehistory

Sometime around 1965-7 Walter Greiner recognizes the need to understand the atomic structure of superheavy element Z=164.
Greiner: The important thing is that for $Z = 80$ you have $Z\alpha$ less than unity, but for super-heavy nuclei around $Z = 164$ it is suddenly larger than unity and you do not know whether the expansion in $Z\alpha$ converges anymore. You really have to start from a completely different point of view and develop new methods.

Greiner: I would like to stress that this quantum electrodynamic problem is very interesting from a purely theoretical point of view. I mean no matter whether we can make nuclei with $Z = 164$ or not, it is interesting in itself to study theoretically what really happens. If however elements around $Z = 164$ were very unstable the problem would be merely academic.

We may ask ourselves what we may further learn from super-heavy nuclei. Let me mention a few other important aspects. I certainly do not have to convince you that there is nothing to learn about basic nuclear forces - let's forget this completely.
1\textsuperscript{st} step: Dirac relativistic QM Singularity

Interior Electron Shells in Superheavy Nuclei
submitted August 14 1968

Strong Fields in High Z Atoms

Single Particle Dirac Equation

\[(\bar{\alpha} \cdot i \vec{\nabla} + \beta m + V(r))\psi_n(\vec{r}) = E_n \psi_n(\vec{r})\]

\[V(r) = \begin{cases} 
\frac{-Z\alpha}{r} & r > R_N \\
-\frac{3}{2} \frac{Z\alpha}{R_N} + \frac{r^2}{2} \frac{Z\alpha}{R_N^3} & r < R_N
\end{cases}\]

Key feature: bound states pulled from one continuum move as function of $Z\alpha$ across into the other continuum.
The 1968 October revolution: Walter Greiner teaches theoretical physics in 1st semester, & starts new strong fields research group.
2nd step: Walter's great invention

Embedding a super bound electron in positron continuum

Solution of the Dirac Equation for Strong External Fields*

Berndt Müller, Heinrich Peitz, Johann Rafelski, and Walter Greiner
Institut für Theoretische Physik der Universität Frankfurt, Frankfurt am Main, Germany
(Received 14 February 1972)

The 1s bound state of superheavy atoms and molecules reaches a binding energy of $-2mc^2$ at $Z \approx 169$. It is shown that the $K$ shell is still localized in $r$ space even beyond this critical proton number and that it has a width $\Gamma$ (several keV large) which is a positron escape width for ionized $K$ shells. The suggestion is made that this effect can be observed in the collision of very heavy ions (superheavy molecules) during the collision.
What is (mostly) this about?

The bound states drawn from one continuum move as function of $Z$ across into the other continuum. **Mix-up of particle/antiparticle states**

3rd step: 1972 HI Collisions replace the need for super-super-heavy nuclei

HI collisions: electrons inquasimolecular yields
A decade of process computation in heavy ion collisions

Probing QED Vacuum with Heavy Ions

Johann Rafelski, Johannes Kirsch, Berndt Müller, Joachim Reinhardt and Walter Greiner

Abstract We recall how nearly half a century ago the proposal was made to explore the structure of the quantum vacuum using slow heavy-ion collisions. Pursuing this topic we review the foundational concept of spontaneous vacuum decay accompanied by observable positron emission in heavy-ion collisions and describe the related theoretical developments in strong fields QED.
4th step 1973: no stable vacuum, hence vacuum decay in Strong Fields


THE CHARGED VACUUM IN OVER-CRITICAL FIELDS

J. RAFELSKI, B. MÜLLER and W. GREINER
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Received 4 June 1973
(Revised 17 September 1973)

Abstract: The concept of over-critical fields, i.e. fields in which spontaneous, energy-less electron-position pair creation may occur, is discussed. It is shown that only a charged vacuum can be a stable ground state of the overcritical field. The time-dependent treatment confirms previous results for the cross sections for the auto-ionizing positrons. The questions in connection with the classical Dirac wave functions in over-critical fields are extensively discussed in the frame of the self-consistent formulation of QED including the effects of vacuum polarization and self-energy.
Stabilization of local vacuum state

Speed of decay of false vacuum controlled by (Heisenberg-Schwinger mechanism) E-field strength

There is localized charge density in the vacuum, not a particle of sharp energy. Formation of the charged vacuum ground state observable by positron emission: which fills any vacancies among ‘dived’ states in the localized domain.

The Decay of the Vacuum

by Lewis P. Fulcher, Johann Rafelski and Abraham Klein

Near a superheavy atomic nucleus empty space may become unstable, with the result that matter and antimatter can be created without any input of energy. The process might soon be observed experimentally.

Stabilization of the Charged Vacuum Created by Very Strong Electrical Fields in Nuclear Matter*

Berndt Müller and Johann Rafelski
(Received 2 December 1974)

The expectation value of electrical charge in charged vacuum is calculated utilizing the Thomas–Fermi model. We find almost complete screening of the nuclear charge. For any given nuclear density there is an upper bound for the electrical potential. For normal nuclear densities this value is –250 MeV. This suggests that the vacuum is stable against spontaneous formation of heavy, charged particles.
Miklos was invited to join Frankfurt effort

Phys. Rev. Lett. 33, 921 – Published 7 October 1974

Vacuum Polarization in Heavy-Ion Collisions

Miklos Gyulassy  Received 5 August 1974

The results of a study on vacuum polarization, orders $\alpha(Z\alpha)^n$, $n \geq 3$, for large-Z systems encountered in heavy-ion collisions are presented. It is shown that the higher-order vacuum polarization cannot prevent the $1S_{\frac{1}{2}}$ state from reaching the lower continuum, $E = -m_e c^2$, for some critical charge $Z_{cr} \sim 170$. In addition, the stability and localization of a heliumlike system for $Z > Z_{cr}$ is demonstrated.

Nuclear Physics A Volume 244, Issue 3, 16 June 1975, Pages 497-525

Higher order vacuum polarization for finite radius nuclei ⭐

Miklos Gyulassy  Lawrence Berkeley Laboratory, University of California, Berkeley, California 94720 USA

Received 8 October 1974, Revised 25 November 1974

The calculation of the higher order, $\alpha(Z\alpha)^n$, $n \geq 3$, vacuum polarization charge density induced by high-Z nuclei of finite extent is discussed here. The Wichmann-Kroll formalism relating the vacuum polarization charge density to the Green function of the Dirac equation is reviewed with attention drawn to modifications necessary for very large-Z systems ($Z > 137$) encountered in heavy ion collisions. This paper is concerned with the construction of the radial Green functions for the Dirac equation in the field of finite radius nuclei and on the numerical calculation of the higher order vacuum polarization density from those Green functions. Specific calculations are made for muonic Pb and superheavy electronic atoms. The results from these calculations have been published elsewhere but are further elaborated upon here.
Back to Frankfurt timeline: 5\textsuperscript{th} Step

“Accelerated” Vacuum – compare BH

Recognize external fields as a TEMPERATURE

INTERPRETATION OF EXTERNAL FIELDS AS TEMPERATURE*

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Received 5 September 1977
1. Introduction

The structure of the vacuum is one of the most important topics in modern theoretical physics. In the best understood field theory, Quantum Electrodynamics (QED), a transition from the neutral to a charged vacuum in the presence of strong external electromagnetic fields is predicted. This transition is signalled by the occurrence of spontaneous $\gamma^+\gamma^-$ pair creation. The theoretical implications of this process as well as recent successful attempts to verify it experimentally using heavy ion collisions are discussed. A short account of the history of the vacuum concept is given. The role of the vacuum in various areas of physics, like gravitation theory and strong interaction physics is reviewed.

1.1 The Charged Vacuum

Our ability to calculate and predict the behaviour of charged particles in weak electromagnetic fields is primarily due to the relative smallness of the fine-structure constant $\alpha = 1/137$. However, physical situations exist in which the coupling constant becomes large, e.g. an atomic nucleus with $Z$ protons can exercise a much stronger electromagnetic force on the surrounding electrons than could be described in perturbation theory, and hence it is foreseeable that the new expansion parameter $(Z\alpha)$ can quite easily be of the order of unity. In such cases nonperturbative methods have to be used to describe the resultant new phenomena, of which the most outstanding is the massive change of the ground-state structure, i.e. of the vacuum of quantum electrodynamics.
Jobs accomplished: Visby 1986
Return 30 years after:

Magnetic anomalies motivate

LHC RHI collisions with extreme B-fields

Magnetic stars (magnetars) with common extreme magnetic properties

Obtain classical and QM description of neutral particles with magnetic moment
Glimpse on anomalous magnetic moment challenges

Dirac-Puli

\[ E_{DP} = \pm \sqrt{\left( m^2c^4 + 2e\hbar c B \lambda_L - \frac{eB\hbar}{2mc}(g - 2)s \right)^2 + p_z^2c^2} \]

Landau level quantum number

\[ \lambda_L = n + \frac{1}{2} - s \]

which has values \( \lambda_L = 0, 1, 2 \ldots \)

Klein-Gordon-Pauli

\[ E = \pm \sqrt{ m^2c^4 + p_z^2c^2 + 2e\hbar c B \left( n + \frac{1}{2} - \frac{g}{2}s \right) } \]

Diagram of KGP-Landau levels for particles with zero z-component momentum.

- \( n + \frac{1}{2} \)
- \( s = \pm 1/2 \)
- \( a > 0 \)

- 3/2
- 1/2
- 0
1/r-Coulomb problem

The energy levels of the KGP-Coulomb equation are

\[ E_{\pm \lambda}^{n, j} = \frac{mc^2}{\sqrt{1 + \frac{Z^2\alpha^2}{(n_r + 1/2 + \nu)^2}}} , \]  

\[ \nu = \sqrt{(\lambda \pm 1/2)^2 + \left(\frac{g^2}{4} - 1\right) Z^2\alpha^2} , \]  

\[ \lambda = \sqrt{(j + 1/2)^2 - \frac{g^2}{4} Z^2\alpha^2} . \]  

Using Eq. (c) in Eq. (b) we can also write

\[ \nu = \sqrt{(j + 1/2)^2 + (1/2)^2 - Z^2\alpha^2 \pm \lambda} \]  

This clarifies that eigenvalues Eq. (a) are analytic functions of the two independent couplings \( Z\alpha \) and \( gZ\alpha \) seen in the original form of the KGD equation, and, \( gZ\alpha \) is now only appearing in \( \lambda \).
\[ \mathcal{L}_{EH} = \frac{1}{8\pi^2} \int_0^\infty \frac{ds}{s^3} e^{-im^2 s} \left( \frac{eas \cosh \left[ \frac{g}{2} eas \right]}{\sinh [eas]} \frac{ebs \cos \left[ \frac{g}{2} ebs \right]}{\sin [ebs]} - 1 \right) \]

|g| < 2 \quad a^2 - b^2 = \mathcal{E}^2 - \mathcal{B}^2 = 2S \quad ab = \mathcal{E} \cdot \mathcal{B} = P

\[ \mathcal{L}_{EH} = \frac{m^2 T}{16\pi^2} \int_0^\infty dE \ln \left[ E^2 - m_-^2 \right] \sum_{i \epsilon} \ln \left[ 1 + e^{\pm i \pi \frac{g}{2} e^{-E/T}} \right], \quad T = \frac{e\mathcal{E}}{m_\pi}, \]

\[ E_n = \pm \sqrt{m^2 + p_z^2 + Q|eB|[(2n + 1) \mp g/2]}, \]

where \( Q = \pm 1 \). Summing orbit quantum number \( n \), we see that a shift \( g \to g + 4k \) corresponds to a shift in \( n \), leaving the summed states unchanged

\[ \mathcal{L}_{EH}(g_k) = \mathcal{L}_{EH}(g_{k - 1}), \]

At magnetic field strengths beyond

\[ |eB| < \frac{m_-}{|g/2 - 1|} \sim 862m^2, \quad g = g_f(0) = 2.002319, \]

the energies become imaginary. We limit

\[ \mathcal{L}_{EH}(a, b, g) \text{ is depicted as a function } b/a. \text{ Dashed line shows rescaled mass} \]

\[ \tilde{m}^2 = m^2 + \left| \frac{g_k - 4k}{2} \right| - 1 |b| \]
Job is just beginning:

Now we know: Magnetic moment + strong field can made difference: Introduce Field dependent $m(B)$, $g(B)$

Study both real and imaginary part of $\text{Leff}$:
Strong field vacuum modifications, seek possible new magnetar ground state
What-if: Quark Confinement is a vacuum structure effect?
Interest turns to strong interactions and vacuum structure
1974 first local vacuum structure model of quark confinement inside hadrons

New extended model of hadrons

A. Chodos, R. L. Jaffe, K. Johnson, C. B. Thorn, and V. F. Weisskopf
Phys. Rev. D 9, 3471 – Published 15 June 1974  Received 25 March 1974
DOI: https://doi.org/10.1103/PhysRevD.9.3471

ABSTRACT

• Quarks live inside a domain where the (perturbative) vacuum is without gluon fluctuations. This outside structure wants to enter, but is kept away by quarks trying to escape.
• The model assumes that the energy density $E/V=0$ of the true vacuum is lower than that inside of a hadron.
Experiment: melt the vacuum structure

- $T < \sim 10^3 \text{ K} \quad \Rightarrow \text{molecules intact}$
  $T > \sim 10^3 \text{ K} \ (0.1 \text{ eV}) \quad \Rightarrow \text{molecular dissociation}$

- $T < \sim 10^4 \text{ K} \quad \Rightarrow \text{atoms intact}$
  $T > \sim 10^4 \text{ K} \ (1 \text{ eV}) \quad \Rightarrow \text{atomic ionization, plasma formation}$

- $T < \sim 10^9 \text{ K} \quad \Rightarrow \text{nuclei intact}$
  $T > \sim 10^9 \text{ K} \ (0.1 \text{ MeV}) \quad \Rightarrow \text{nuclear reactions}$

- $T < \sim 10^{12} \text{ K} \quad \Rightarrow \text{protons intact}$
  $T > \sim 10^{12} \text{ K} \ (150 \text{ MeV}) \quad \Rightarrow \text{vacuum melts, quarks free}$

- $T < \sim 10^{15} \text{ K} \quad \Rightarrow \text{electromagnetic and weak interactions separate}$
  $T > \sim 10^{15} \text{ K} \ (150 \text{ GeV}) \quad \Rightarrow \text{Higgs vacuum melts, all quarks massless}$
Melting the QCD vacuum in Nuclear Collisions at Relativistic energy $E \gg Mc^2$

![Diagram showing Micro-Bang process]

<table>
<thead>
<tr>
<th>Big-Bang</th>
<th>Micro-Bang</th>
</tr>
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<tbody>
<tr>
<td>$\tau \approx 10\mu s$</td>
<td>$\tau \approx 4 \times 10^{-23} s$</td>
</tr>
<tr>
<td>$N_b / N \approx 10^{-10}$</td>
<td>$N_b / N \approx 0.1$</td>
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</table>
Strangeness Signature of QGP
Vacuum Determines Laws of Physics and the Nature of the Universe
Color confinement due to gluon fluctuations

- QCD induces chromo-electric and chromo-magnetic fields throughout space-time – the vacuum is in its lowest energy state, yet it is strongly structured. Fields must vanish exactly everywhere: $\langle H \rangle = 0$

- This is an actual computation of the four-d (time +3-dimensions) structure of the gluon-field configuration. The volume of the box is 2.4 by 2.4 by 3.6 fm, big enough to hold a couple of protons.

- Derek B. Leinweber's group (U Adelaide)

Numerical Method used: lattice in space time

Square of fields does not average out: “condensates

$$\langle \bar{q}q \rangle = (235 \text{ MeV})^3, \langle \frac{\alpha_s}{\pi} G_{\mu\nu} G^{\mu\nu} \rangle = (335 \text{ MeV})^4$$
Quantum Chromo-Dynamics (QCD): Quark colour field lines confined

Most of the mass of visible matter is due to QCD -
Origin of Forces and Nature of Mass, Stability of Matter

- “Elementary” masses are generated by the vacuum. Two dominant mechanisms:
  - Higgs vacuum: \( <H> = h = 246 \text{ GeV} \);
  - \( m_{\text{higgs}} = h/2 \) (?); defines mass for W, Z; top, bottom, charm(?), contributes to lighter particle mass

- QCD vacuum latent heat at the level of \( <E_{V_p}> = 0.3 \text{ GeV} =: \) nuclear mass scale, quarks get constituent mass and are confined. QCD vacuum structure provides +95% of mass of matter

\[
\begin{align*}
m_e c^2 &= 0.511 \text{MeV} & m_N c^2 &= 0.940 \text{GeV} \\
(\text{EM mass!}) & & (\text{QCD mass})
\end{align*}
\]

Units are G=giga, M=mega e=electron charge, V=Volt.

Wigner RCP 19.6.18 Johann Rafelski, Arizona 43
How was matter created?

Matter emerges from quark-gluon plasma

After the Big-Bang the “vacuum” was different till about at 30 μs – expansion cooled the temperature T to a value at which vacuum changed and our matter “froze out”. At that time the density of matter was about ~10^{16} gm / cm^3 (energy density ~ 10 GeV / fm^3, well above that of the center of neutron stars, that is ~60 times nuclear energy density), and temperature was T ~ 160 MeV, that is ~ 2 \times 10^{12} K.
Do we live in False vacuum?

Dark Energy: (unlike dark matter) a property of the vacuum indicating we are not in ground state in the Universe (could be the case near to matter).
Dynamical emergence of the Universe into the false vacuum

Johann Rafelski and Jeremiah Birrell

Department of Physics, University of Arizona,

Abstract. We study how the hot Universe evolves and acquires the prevailing vacuum state, demonstrating that in specific conditions which are believed to apply, the Universe becomes frozen into the state with the smallest value of Higgs vacuum field $v = \langle h \rangle$, even if this is not the state of lowest energy. This supports the false vacuum dark energy $\Lambda$-model. Under several likely hypotheses we determine the temperature in the evolution of the Universe at which two vacua $v_1, v_2$ can swap between being true and false. We evaluate the dynamical surface pressure on domain walls between low and high mass vacua due to the presence of matter and show that the low mass state remains the preferred vacuum of the Universe.

1 Introduction

This work presents relatively simple arguments for why the cosmological evolution selects the vacuum with smallest Higgs VEV $v = \langle h \rangle$ which, in general, could be and likely is the ‘false’ vacuum. Our argument relies on the Standard Model (SM) minimal coupling $m \to gh$, or similar generalizations in ‘beyond’ SM (BSM), so that the vacuum with the smallest Higgs VEV also has the smallest particle masses. In anticipation of the model with multiple vacua, we call the vacuum state with lowest free energy at temperature $T$ ‘the true vacuum’ and all others ‘the false vacuum’. Note that this is a temperature dependent statement: we live today in the false vacuum which as we will show was once the true vacuum.

In the presence of pairs of particles and antiparticles at high temperature the vacuum state with smallest $v$ is energetically preferred, even if it has a large vacuum energy. This is so because smaller $v$ implies smaller particle masses and hence less energy, and free energy, in the particle distributions. By the time the Universe cools sufficiently for the larger vacuum energy to dominate the smaller particle free energies, the probability of swap to the large mass true vacuum is vanishingly small in general.

Therefore, the Higgs minimum with the lowest value of the Higgs field $v$, and thus not necessarily the lowest value of the effective potential $W(v) = (V/\langle h \rangle)$, emerges as the prevalent vacuum in our Universe. The difference, $\rho_4 = \Delta W$, between the prevalent vacuum state today and the true minimum is a natural candidate to explain the observed dark energy density.

$$\rho_4 = 25.6 \text{ meV}^4.$$  (1.1)
The vacuum and symmetry breaking

\[ \langle H \rangle = 0 \]

\[ \langle H \rangle \neq 0 \]

Normal, “Higgs” and False Vacuum

Fluctuations

Vacuum energy

Release in vacuum decay
All of this and more in....
Critical Fields = \textbf{Critical Acceleration} with Radiation Reaction
Critical Fields =

Critical Acceleration

An electron in presence of the critical ‘Schwinger’ (Vacuum Instability) field strength of magnitude:

\[ E_s = \frac{m_e^2 c^3}{e\hbar} = 1.323 \times 10^{18} \text{ V/m} \]

is subject to critical natural unit =1 acceleration:

\[ a_c = \frac{m_e c^3}{\hbar} \rightarrow 2.331 \times 10^{29} \text{ m/s}^2 \]

Truly dimensionless unit acceleration arises when we introduce specific acceleration

\[ \Xi = \frac{a_c}{mc^2} = \frac{c}{\hbar} \]

Specific unit acceleration arises in Newton gravity at Planck length distance:

\[ \Xi_G \equiv G/L_p^2 = c/\hbar \text{ at } L_p = \sqrt{\hbar G/c}. \]

In the presence of sufficiently strong electric field \( E_s \) by virtue of the equivalence principle, electrons are subject to Planck ‘critical’ force.
Planck units

\[
\begin{align*}
\hbar/k_B &= a = 0.4818 \times 10^{-10} [\text{sec} \times \text{Celsiusgrad}] \\
h &= b = 6.885 \times 10^{-27} [\text{cm}^2 \text{g} \text{r} \text{sec}] \\
c &= c = 3.00 \times 10^8 [\text{cm} \text{sec}] \\
G &= f = 6.685 \times 10^{-8} [\text{cm}^3 \text{g} \text{r} \text{sec}^2]
\end{align*}
\]

Wählt man nun die «natürlichen Einheiten» so, dass in dem neuen Maasssystem jede der vorstehenden vier Constanten den Werth 1 annimmt, so erhält man als Einheit der Länge die Größe:

\[
\sqrt{2\pi} \, l_{Pl} = V_{\hbar/c} = 4.13 \times 10^{-33} \text{cm} 
\]

als Einheit der Masse:

\[
\sqrt{2\pi} \, m_{Pl} = V_{bc/f} = 5.56 \times 10^{-8} \text{g}
\]

als Einheit der Zeit:

\[
\sqrt{2\pi} \, t_{Pl} = V_{\hbar/c^2} = 1.38 \times 10^{-43} \text{sec}
\]

als Einheit der Temperatur:

\[
\sqrt{2\pi} \, T_{Pl} = a V_{c/f} = 3.50 \times 10^{32} \text{Cels}
\]

Diese Grössen behalten ihre natürliche Bedeutung so lange bei, als die Gesetze der Gravitation, der Lichtfortpflanzung im Vacuum und die beiden Hauptsätze der Wärmetheorie in Gültigkeit bleiben, sie müssen also, von den verschiedensten Intelligenzen nach den verschiedensten Methoden gemessen, sich immer wieder als die nämlichen ergeben.

"These scales retain their natural meaning as long as the law of gravitation, the velocity of light in vacuum and the central equations of thermodynamics remain valid, and therefore they must always arise, among different intelligences employing different means of measuring."  

M. Planck, "Über irreversible Strahlungsvorgänge." Sitzungsberichte der Königlich Preußischen Akademie der Wissenschaften zu Berlin 5, 440-480 (1899), (last page)
Critical acceleration probably achieved at RHIC

Two nuclei smashed into each other from two sides: components ‘partons’ can be stopped in CM frame within $\Delta \tau \approx 1$ fm/c. Tracks show multitude of particles produced, as observed at RHIC (BNL).

- The acceleration $a$ achieved to stop some/any of the components of the colliding nuclei in CM: $a \approx \frac{\Delta y}{M_i \Delta \tau}$. Full stopping: $\Delta y_{\text{SPS}} = 2.9$, and $\Delta y_{\text{RHIC}} = 5.4$. Considering constituent quark masses $M_i \approx M_N/3 \approx 310$ MeV we need $\Delta \tau_{\text{SPS}} < 1.8$ fm/c and $\Delta \tau_{\text{RHIC}} < 3.4$ fm/c to exceed $a_c$.

A new path to probing space time

The new idea is to collide kJ pulses with themselves or with particles, with light intense enough to crack the vacuum

Pair e+e- production
EM fields polarize quarks in QCD vacuum

On the way we can study nonlinear QED

Should we be able to focus of 5kJ to 10% atom size we reach energy density of QGP. Macroscopic domain of early Universe

...and if we get that energy into proton sized volume the Higgs vacuum will melt
Strong Field Unsolved Problem
Radiation-Acceleration-Reaction

Conventional Lorentz-Electromagnetic force is incomplete: accelerated charged particles can radiate: “radiation friction” instability – some acceleration produces friction slowdown, produces more slowdown etc. Need acceleration that is not negligible to explore the physics of radiation friction. Problem known for 115 years.

Microscopic justification in current theory (LAD)
1) Inertial Force = Lorentz-force with friction - > get world line of particles=source of fields
2) Source of Fields = Maxwell fields - > get fields, and omit radiated fields
3) Fields fix Lorentz force with friction - > go to 1.

So long as the radiated fields are small, we can modify the Lorentz Force to account for radiated field back reaction. The “Lorentz-Abraham-Dirac (LAD)” patch is fundamentally inconsistent, and does not follow from an action principle. Many other patches exist, some modifying inertia, others field part of Lorentz force - it introduces a nonlinear and partially nonlocal Lorentz-type force. No action principle is known.
Radiation reaction regime

Deviations from Lorentz force impact significantly Lorentz dynamics in dark shaded area of the $\gamma, a_0$ plane

<table>
<thead>
<tr>
<th></th>
<th>Electron</th>
<th>Laser</th>
<th>X/Gamma</th>
</tr>
</thead>
<tbody>
<tr>
<td>Energy</td>
<td>.1 – 5 GeV</td>
<td>J and kJoule</td>
<td>MeV</td>
</tr>
<tr>
<td>Duration</td>
<td>1-10 fs</td>
<td>20 – 150 fs</td>
<td>10 – 1000 fs</td>
</tr>
<tr>
<td>Rep.rate</td>
<td>10Hz</td>
<td>10Hz</td>
<td>10Hz</td>
</tr>
</tbody>
</table>
SLAC’95 experiment below critical acceleration

\[ p_0^0 = 46.6 \text{ GeV}; \text{ in 1996/7 } a_0 = 0.4, \quad \left| \frac{du^\alpha}{dT} \right| = 0.073 [m_e] \text{ (Peak)} \]

Multi-photon processes observed:
- Nonlinear Compton scattering
- Breit-Wheeler electron-positron pairs


Probing super-critical (Planck) acceleration
\[ a_c = 1 \Rightarrow m_e c^3 / \hbar = 2.331 \times 10^{29} \text{m/s}^2 \]

Plan A: Directly laser accelerate electrons from rest, requires Schwinger scale field and may not be realizable — backreaction and far beyond today’s laser pulse intensity technology.

Plan B: Ultra-relativistic Lorentz-boost: we collide counter-propagating electron and laser pulse.
Pulse Lorentz Transform (LT)

Relativistic electron-laser pulse collision

\[ u^\beta = \gamma(1, \vec{v}) \rightarrow \text{In electron's rest frame: } u'_\beta = (1, \vec{0}) \]

Doppler shift: \[ \omega' = \gamma(1 + \vec{n} \cdot \vec{v}) \omega \]

Unit acceleration condition: \[ a_0 \frac{\omega'}{m_e} \approx 2 \gamma a_0 \frac{\omega}{m_e} \rightarrow 1 \]
Example: Electron de-acceleration by a pulse

Lorentz invariant acceleration \( \sqrt{-u^\alpha u_\alpha} \) \( [m_e] \) function of time

Red: solution of Lorentz equation

Collision between a circularly polarized square plane wave with \( a_0 = 100 \) and initial \( E_e = 0.5 \text{ GeV}, \gamma = 1,000 \) electron,

# Sample of proposed LAD extensions

<table>
<thead>
<tr>
<th>LAD</th>
<th>Equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Landau-Lifshitz</td>
<td>( \mu^\alpha = qF^\alpha_\beta u_\beta + m\tau_0 \left[ \ddot{u}^\alpha + u^\beta \dot{u}^{\beta*} u^\alpha \right] )</td>
</tr>
<tr>
<td>Caldirola</td>
<td>( 0 = qF^\alpha_\beta , (\tau) , u_\beta (\tau) + \frac{m}{2\tau_0} \left[ u^\alpha (\tau - 2\tau_0) - u^\alpha (\tau) , u_\beta (\tau) , u^\beta (\tau - 2\tau_0) \right] )</td>
</tr>
<tr>
<td>Mo-Papas</td>
<td>( \mu^\alpha = qF^\alpha_\beta u_\beta + q\tau_0 \left[ F^\alpha_\beta , \dot{u}<em>\beta + F^\alpha</em>\gamma , \dot{u}_\beta , u^\gamma \right] )</td>
</tr>
<tr>
<td>Eliezer</td>
<td>( \mu^\alpha = qF^\alpha_\beta , (\tau) , u_\beta (\tau) + \frac{m}{\tau_0} \left[ u^\alpha (\tau - \tau_0) - u^\alpha (\tau) , u_\beta (\tau) , u^\beta (\tau - \tau_0) \right] )</td>
</tr>
<tr>
<td>Caldirola-Yaghjian</td>
<td>( \mu^\alpha = qF^\alpha_\beta , (\tau) , u_\beta (\tau) + \frac{m}{\tau_0} \left[ u^\alpha (\tau - \tau_0) - u^\alpha (\tau) , u_\beta (\tau) , u^\beta (\tau - \tau_0) \right] )</td>
</tr>
</tbody>
</table>

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Other recent references
**Insight:**

To resolve inconsistencies: we need to formulate a NEW “large acceleration” theory of electro-magnetism, comprising Mach’s principle, and challenging understanding of inertia.

**THEORY Question:** How to achieve that charged particles when accelerated radiate in self-consistent field – and we need EM theory with Mach principle accounted for (gravity, quantum physics=zero acceleration theories)!

**EXPERIMENT:** strong acceleration required. What is strong: unit acceleration=Heisenberg-Schwinger Field

Is there a limit to how fast we can accelerate electrons to ultra high energy? Example of early Model: Born-Infeld electromagnetism (Frankfurt fame)

Can the empty space remain transparent to a plane wave of arbitrary intensity? And why? **Perfect wave and perfect translational symmetry required.**