Homework #9 for Physics 371

Due Friday, April 1

1) If a particle is in an angular momentum eigenstate $\psi_{\ell m}$, show that

$$\langle L_x \rangle = \langle L_y \rangle = 0$$

Also show that

$$\langle L_x^2 \rangle = \langle L_y^2 \rangle = \frac{\hbar^2}{2} [\ell(\ell+1) - m^2].$$

2) Using the results of problem 1, show that

$$\Delta L_x \, \Delta L_y \geq \frac{\hbar}{2} |\langle L_z \rangle|$$

in the state $\psi_{\ell m}$. For which state(s) $\psi_{\ell m}$, if any, does the *equality* in the above expression hold?

3) Suppose \vec{L}^2 is measured for a system and the value $6\hbar^2$ is obtained. If L_y is measured immediately thereafter, what possible values can result?

4) Show that if a state exists which is a simultaneous eigenstate of \hat{L}_x and \hat{L}_y , this state has eigenvalues $L_x = L_y = L_z = 0$.

5) Show that for a state with angular momentum quantum number ℓ , the angle θ between the angular momentum vector and the z axis obeys

$$|\tan \theta| \ge \ell^{-1/2}$$

6-8) Griffiths 4.1, 4.19, and 4.21.