

Chronology of QM

Max Planck (1901)

Black-body radiation

$$E = nh\nu, \quad n = 0, 1, 2, \dots$$

$$h = 6.62618 \times 10^{-34} \text{ J s}$$

Planck's constant

Einstein (1905)

Photoelectric effect

$$h\nu = W + K.E.$$



Bohr (1913)

Hydrogen atom

$$\mu = \frac{m_e m_N}{m_e + m_N}$$

Assumption: $\mu v r = n \hbar$

$$n = 1, 2, 3, \dots$$

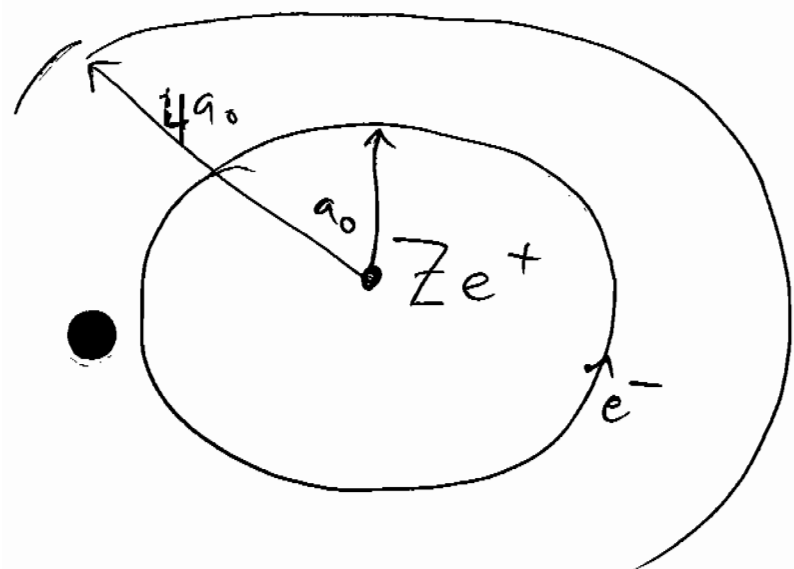
$$\hbar \equiv \frac{h}{2\pi}$$

$$\Rightarrow E_n = - \frac{\mu e^4}{2\hbar^2} \frac{Z^2}{n^2}$$

$$\frac{\mu e^4}{2\hbar^2} = 13.6 \text{ eV}$$

$$r_n = n^2 a_0$$

$$a_0 = \frac{\hbar^2}{\mu e^2} \approx 0.5 \text{ \AA}$$



allowed
circular
orbits

$9a_0 \dots$

Sommerfeld (1915)

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- extended Bohr's model to include elliptical orbits, more general (integrable) systems.

Einstein (1918)

Critique of Bohr-Sommerfeld

- quantization rules — they only work for integrable systems, e.g., not for three-body problem.

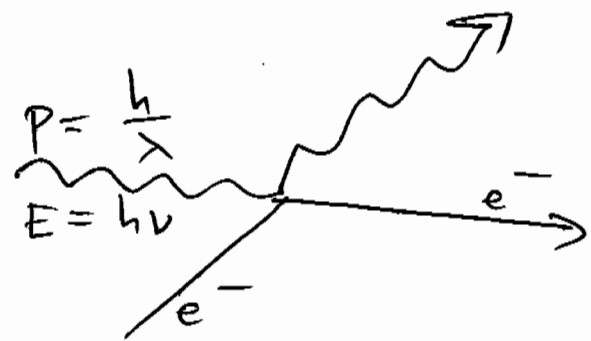
Gutzwiller (1970)

problem for classically

solved Einstein's chaotic systems.

Compton (1923)

Compton scattering



- $$\left. \begin{aligned} p &= \frac{h}{\lambda} \\ E &= h\nu \end{aligned} \right\} \text{photon}$$
 waves behave like particles

de Broglie (1923)

particles behave like waves!

$$p = \frac{h}{\lambda} \quad \text{electron}$$

- Explains Bohr's quantization of angular momentum:

$$mvr = n\hbar$$

$$pr = n\hbar$$

$$\frac{hr}{\lambda} = n\hbar$$

$$\Rightarrow n\lambda = 2\pi r$$

standing waves

● Heisenberg (1925)

matrix mechanics

uncertainty principle

$$\Delta x \Delta p_x \gtrsim \hbar$$

● Schrödinger (1925)

wave mechanics

● Dirac (1927)

Shows approaches of H. & Sch.
are equivalent.

Born, Bohr & Heisenberg (late
1920s)

● Copenhagen interpretation
QM = probabilistic theory

Objections: Einstein et al.