

## Chronology of QM

Max Planck (1901)

Black-body radiation

$$E = nh\nu, \quad n = 0, 1, 2, \dots$$

$$h = 6.62618 \times 10^{-34} \text{ J s}$$

Planck's constant

Einstein (1905)

Photoelectric effect

$$h\nu = W + K.E.$$



# Bohr (1913)

Hydrogen atom

$$\mu = \frac{m_e m_N}{m_e + m_N}$$

Assumption:  $\mu v r = n \hbar$

$n = 1, 2, 3, \dots$

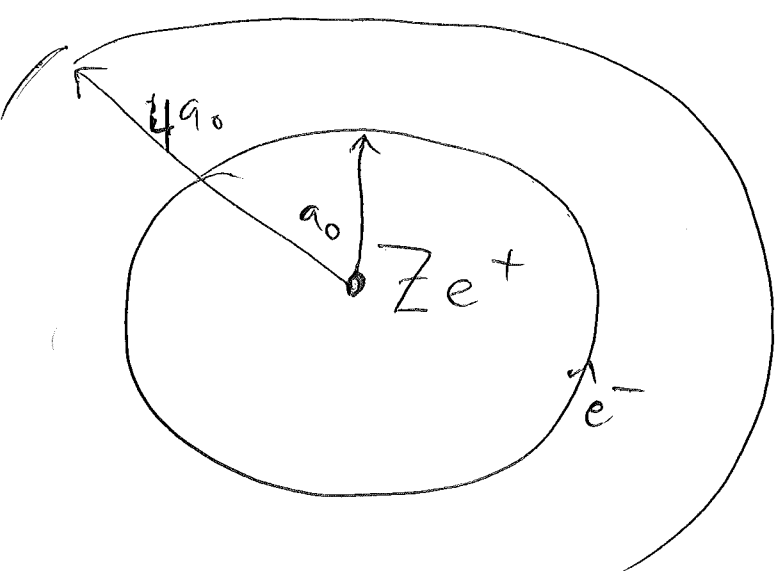
$$\hbar \equiv \frac{h}{2\pi}$$

$$\Rightarrow E_n = - \frac{\mu e^4}{2\hbar^2} \frac{Z^2}{n^2}$$

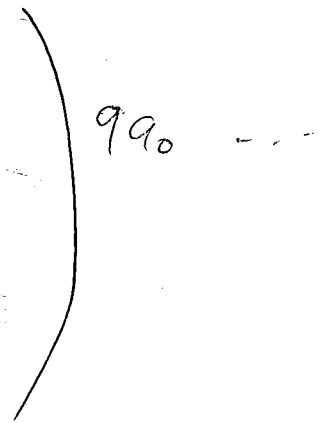
$$\frac{\mu e^4}{2\hbar^2} = 13.6 \text{ eV}$$

$$r_n = n^2 a_0$$

$$a_0 = \frac{\hbar^2}{\mu e^2} \approx 0.5 \text{ \AA}$$



allowed circular orbits



Sommerfeld (1915)

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extended Bohr's model to include elliptical orbits, more general (integrable) systems.

Einstein (1918)

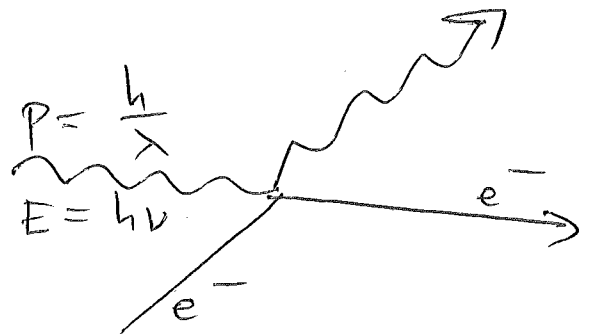
Critique of Bohr-Sommerfeld quantization rules — they only work for integrable systems, e.g., not for three-body problem.

[Gutzwiller (1970) problem for classically

solved Einstein's chaotic systems.]

Compton (1923)

Compton scattering



$$p = \frac{h}{\lambda}$$
$$E = h\nu$$

photon

Waves behave  
like particles

(4)

de Broglie (1923)

particles behave like waves!

$$p = \frac{h}{\lambda} \quad \text{electron}$$

Explains Bohr's quantization of  
angular momentum:

$$mvr = n\hbar$$

$$pr = n\hbar$$

$$\frac{hr}{\lambda} = n\hbar$$

$$\Rightarrow n\lambda = 2\pi r$$

standing waves

Heisenberg (1925)

matrix mechanics

uncertainty principle

$$\Delta x \Delta p_x \geq \frac{\hbar}{2}$$

Schrödinger (1925)

wave mechanics

Dirac (1927)

Shows approaches of H. & Sch. are equivalent.

Born, Bohr & Heisenberg (late 1920s)

Copenhagen interpretation  
QM = probabilistic theory

Objections: Einstein et al.