

Exercises for Physics 472

Problem Set 3; Due 4pm Friday September 19

1–2) Griffiths 5.16, 5.17

3) Conductance of a perfect 2D wire

Using the results for the electrical conductance given in Lecture 4, determine the resistance in Ohms of a perfect two-dimensional wire in the form of a strip of width $D = 4.7\lambda_F$, where λ_F is the de Broglie wavelength of an electron at the Fermi energy. Assume the conduction electrons in the wire can be described by the free-particle Schrödinger equation with Dirichlet boundary conditions (i.e., $\Psi = 0$) along the edges of the strip.

4) Sharvin formula

The Sharvin formula for the electrical conductance of an extremely short contact of area A between two pieces of metal is

$$G \simeq \frac{2e^2}{h} \frac{k_F^2 A}{4\pi}.$$

Derive the Sharvin formula by considering the total current flowing through a hole of area A in a thin insulating barrier separating two free electron gases with different Fermi energies. Use purely macroscopic arguments. Hint: In a free electron gas, the number of electrons with energy between E and $E + dE$ traveling at an angle between θ and $\theta + d\theta$ with respect to a given axis is

$$\frac{\partial^2 n}{\partial E \partial \theta} dE d\theta = \frac{D(E)}{2} \sin \theta dE d\theta,$$

where $D(E)$ is the density of states.